

AI for healthcare

Lecture 1/4 – Introduction

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Thursday, 2pm–5pm – 4 lectures

Epita, rooms KB404 + SM15

Validation: team project + quizz

Who am I? A short CV

Background in **mathematics** and **data sciences**:

2012–2016 ENS Paris, mathematics.

2014–2015 M2 mathematics, vision, learning at ENS Cachan.

2016–2019 PhD thesis in **medical imaging** with Alain Trouvé at ENS Cachan.

2019–2021 **Geometric deep learning** with Michael Bronstein at Imperial College.

2021+ **Medical data analysis** in the HeKA INRIA team (Paris).

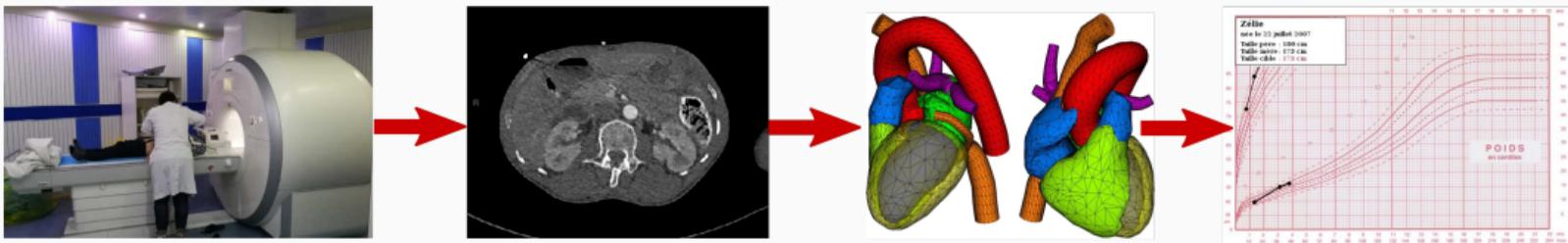
Close ties with **healthcare**:

2015 Image denoising with **Siemens Healthcare** in Princeton.

2019+ MasterClass AI–Imaging, for **radiology interns** in the University of Paris.

2020+ Colloquium on **Medical imaging in the AI era** at the Paris Brain Institute.

My motivation: medical data analysis



Three main **characteristics**:

- **Heterogeneous data**: patient history, images, etc.
- Small stratified samples: 10 – 1 000 patients per group.
- Dealing with **outliers** and the **heavy tails** of our distributions is a priority.

Two main applications – on large real-life datasets

Computational anatomy. 3D medical scans:

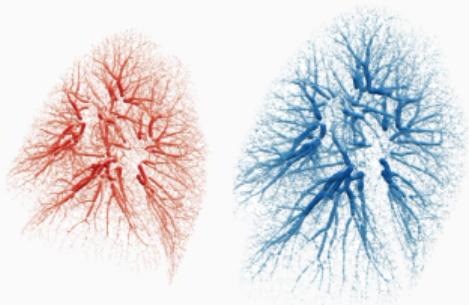
- 100k triangles to represent a brain surface.
- $512 \times 512 \times 512 \simeq 130\text{M}$ voxels for a typical 3D image.

Public health. Over the last decade, medical datasets have **blown up** in size:

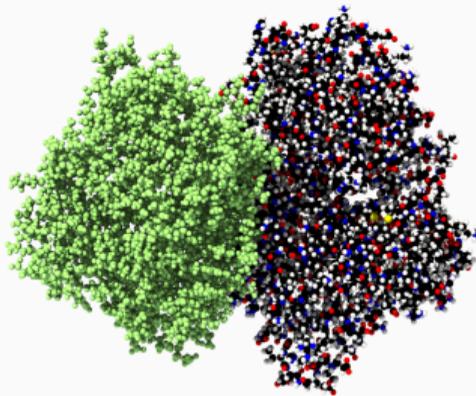
- Clinical trials: **1k patients**, controlled environment.
- UK Biobank: **500k people**, curated data.
- French Health Data Hub: **70M people**, full social security data since ~2000.

Medical doctors, pharmacists and governments need scalable methods.

Some research interests



Optimal transport
for shape registration.



Geometric deep learning
for protein docking.



Survival analysis
for pharmaco-vigilance.

Three points of view on machine learning and AI

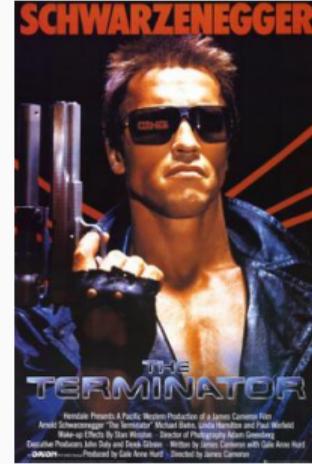
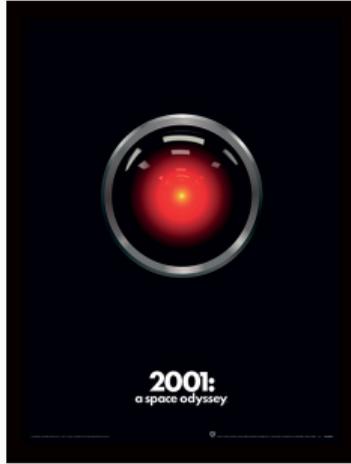
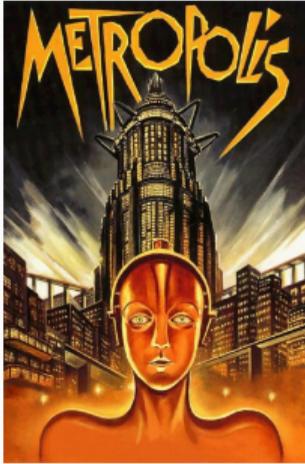
At the intersection of three communities :

- **AI experts** in Paris, London...
- **Students** at the ENS, the MVA, Epita.
- **Medical doctors** among colleagues, friends and family.

AI in healthcare : massive gap between what we **know**,
what we **hope**,
what we **fear**.

What do **you** think?

“Artificial intelligence” is a misleading term



AI seduces, questions, protects or threatens... **But doesn't explain much !**

Among experts, researchers always talk about **models**,
discuss their underlying **hypotheses** and study their **properties**.

The aim of this class is to give you a structured perspective on the field.

Objectives of the class

1. Present a **quick overview** of models that you are likely to encounter.
2. Highlight their underlying **hypotheses, strengths** and **weaknesses**.
3. Provide you with **clear guidelines** on the use of different tools and theories.
4. **Discuss** the realities of applied machine learning.

1. AI = model + data:

- The curse of dimensionality – or why ML is not “just statistics”.
- Example: three levels of analysis in anatomy.

2. How can I choose a good model?

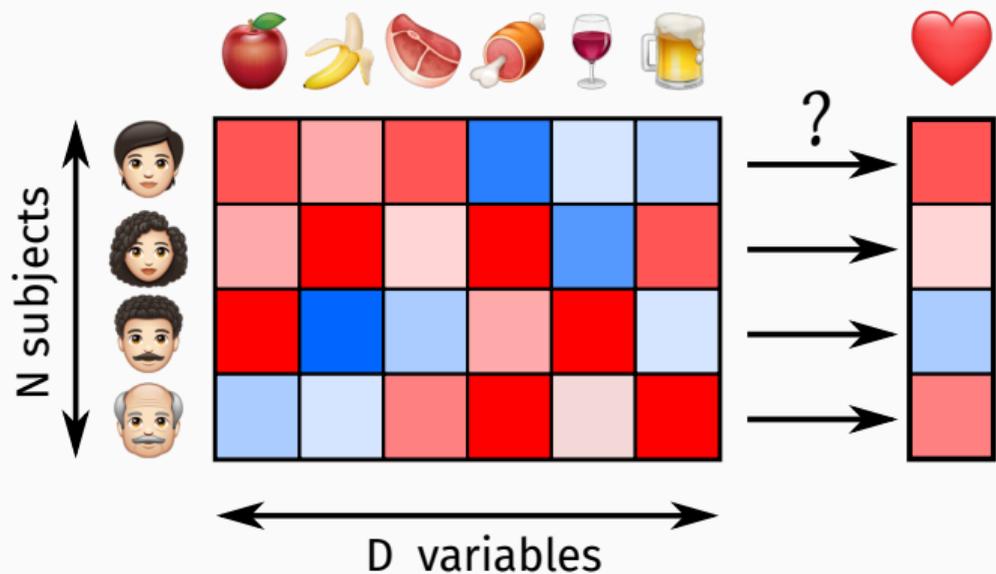
- The map is not the territory.
- Example 1: the sphere of triangles.
- Example 2: style transfer with convolutional neural networks.

3. Overview of the class:

- What’s coming next?
- Setup on the computers.

1. AI = model + data

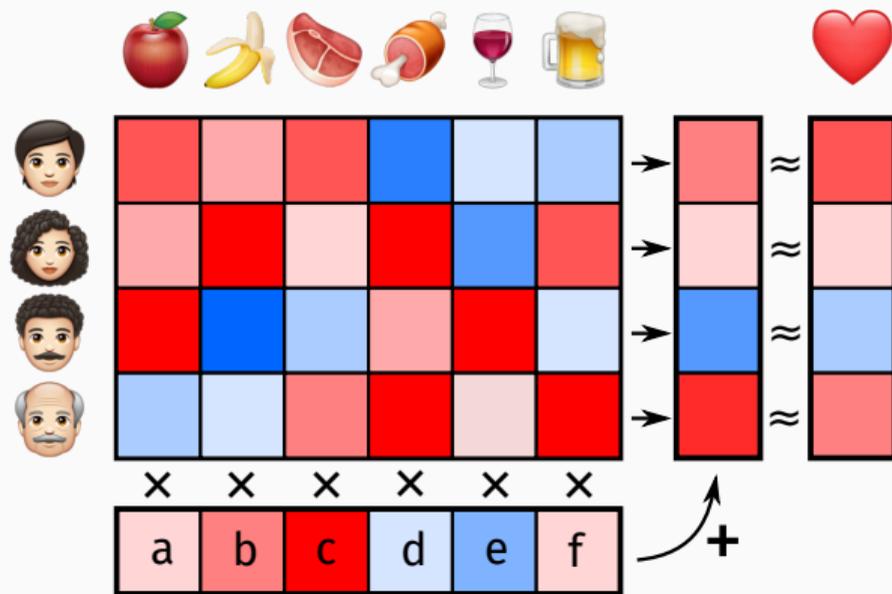
What is a dataset?



Supervised learning = Regression.

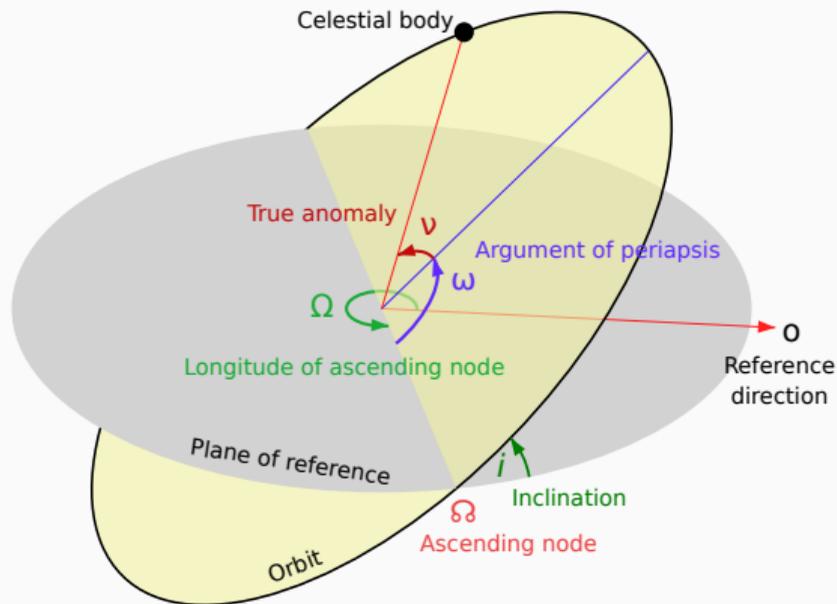
We look for a formula $F(x_1, \dots, x_D)$ of the D variables that best approximates an important quantity (♡).

A simple model: linear regression



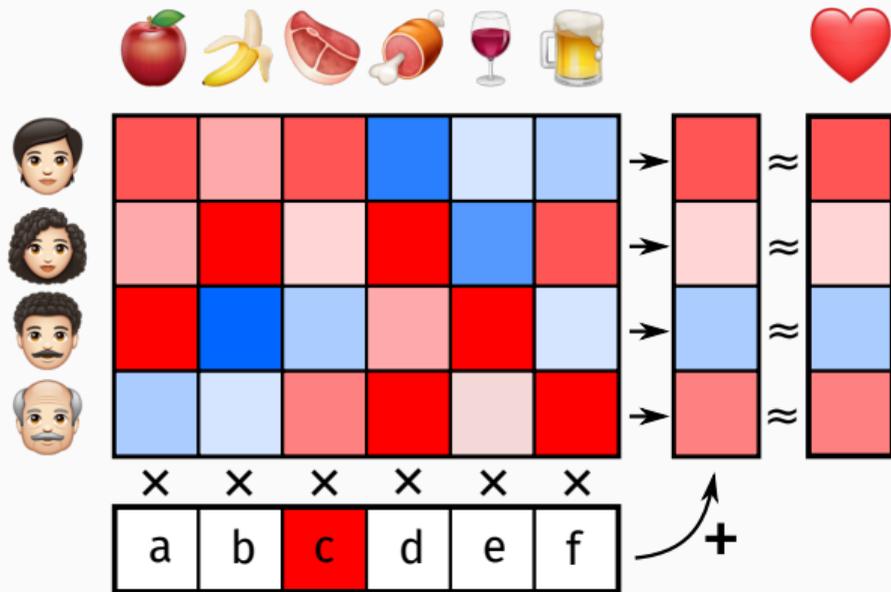
We choose the weights **a**, **b**, ..., **f**
by minimizing a least squares error.

The standard setting of low-dimensional statistics [Las]



First applications to astronomy,
with **hundreds of observations**
on a **handful of variables**.

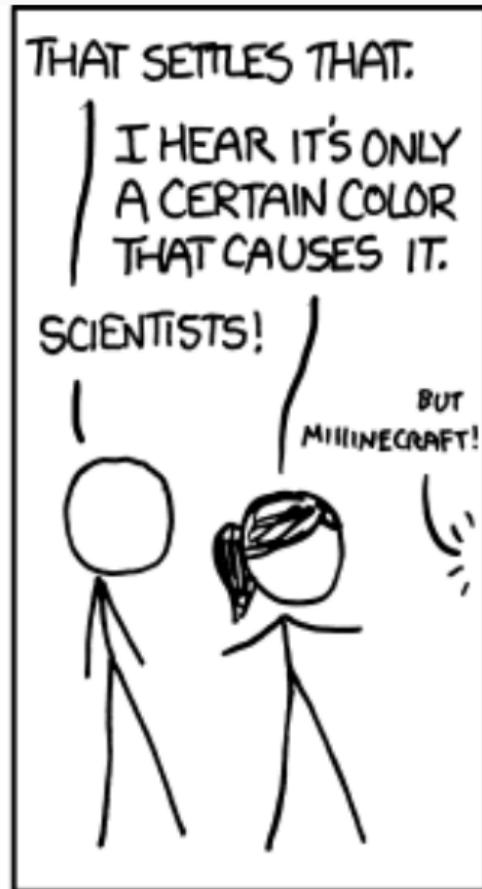
Problem: medicine isn't XIXth century astronomy



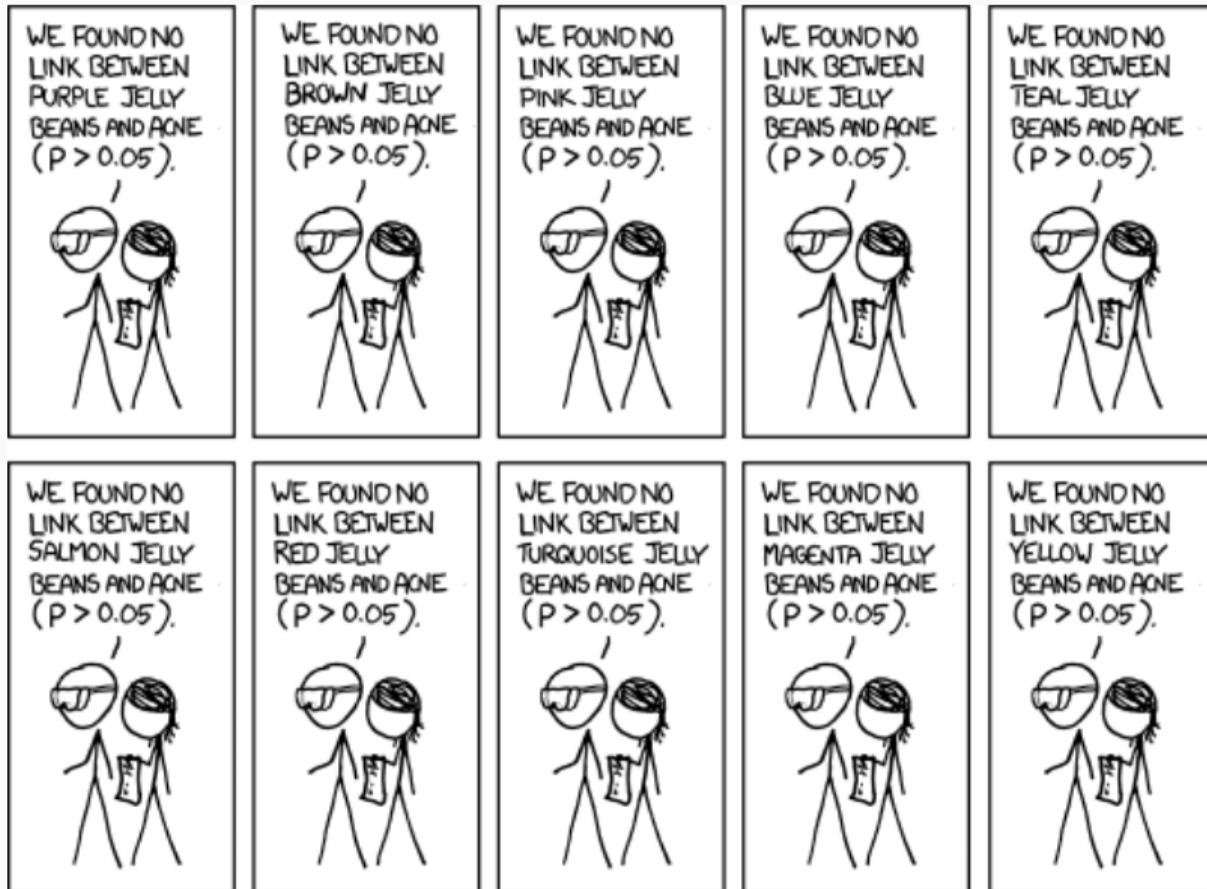
With **lots of information** about **few patients**,
we quickly “discover” spurious correlations.

This is known as **overfitting**.

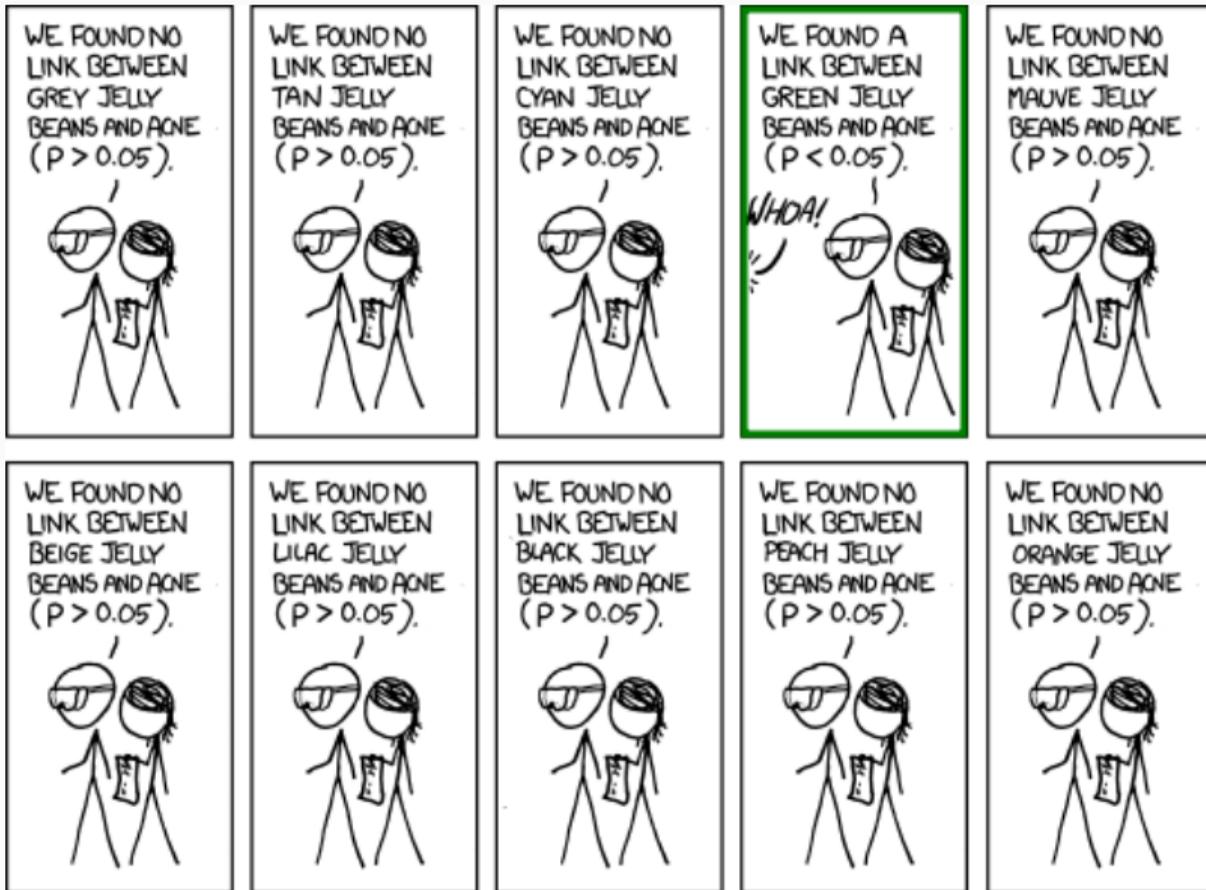
Significant (XKCD 882)

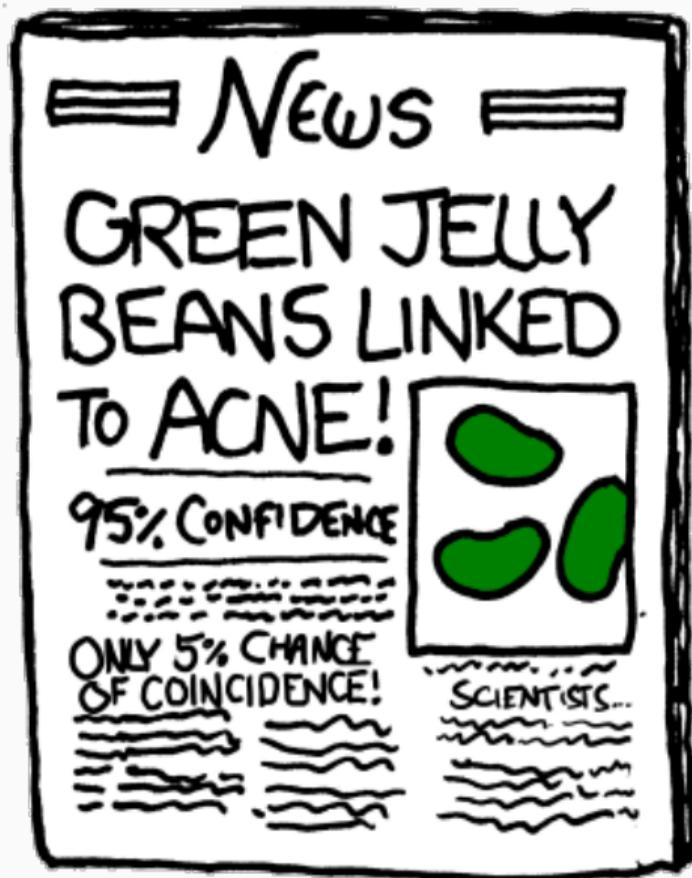


Significant (XKCD 882)



Significant (XKCD 882)





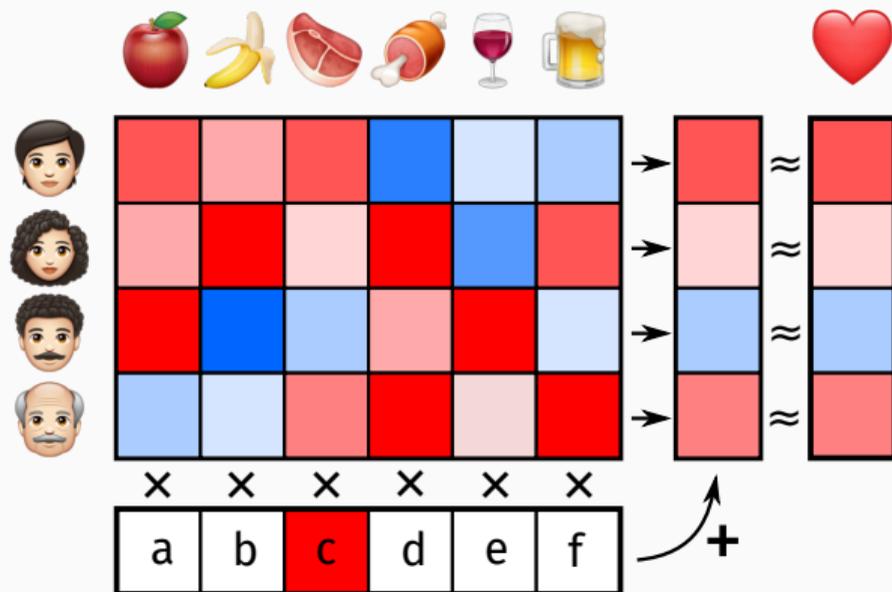
The curse of dimensionality

Having access to **more patients** is usually a **good** thing.
But getting **more information** about each patient is **very dangerous**.

In the previous example: knowing the **color** of the candy led the (imprudent) scientists to **over-interpret** a random fluctuation.

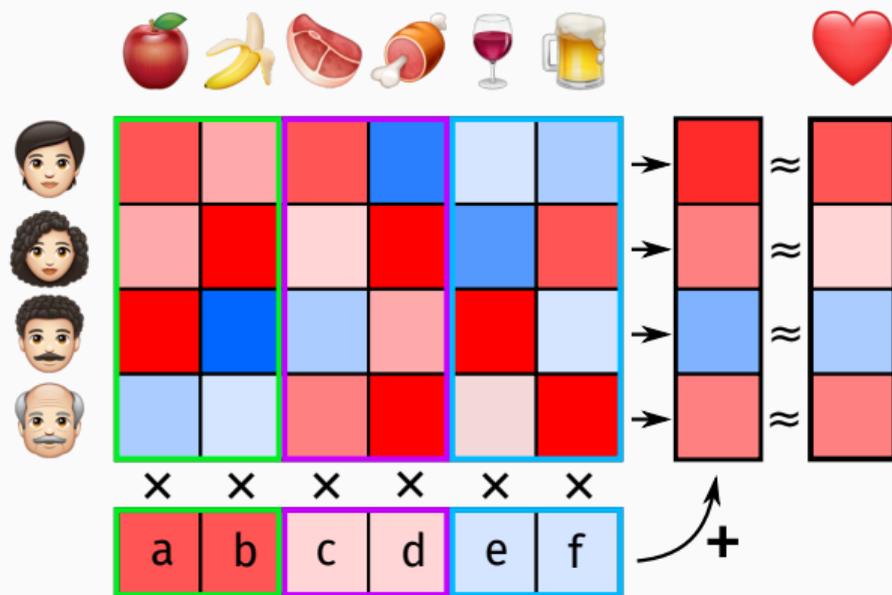
Machine learning is about doing **reliable** statistics
in this dangerous setting.

We must regularize our decision rules – using sparsity



A **sparse** model will select 5 or 10 important columns.
This is useful to handle **tabular data** (XGBoost...)
or **identify sources** in signal processing (Lasso...).

We must regularize our decision rules – using a domain-specific structure

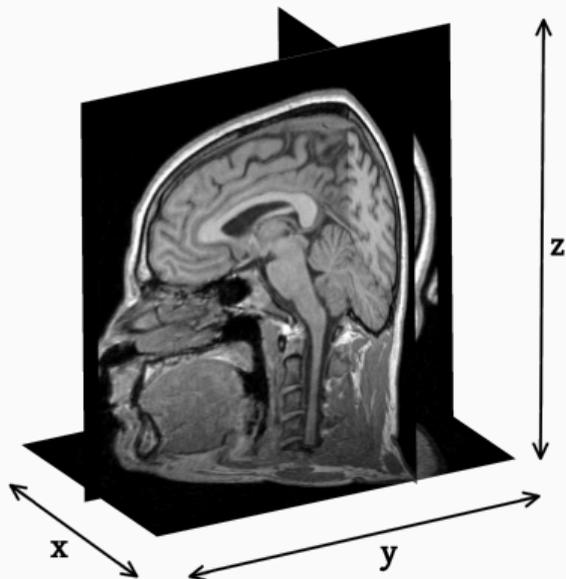


A **structured** model will leverage the **geometry of the data**.

Think about the main **food groups** or the
ATC classification for **medical drugs**.

A first example: medical imaging

A medical image is a massive lump of data

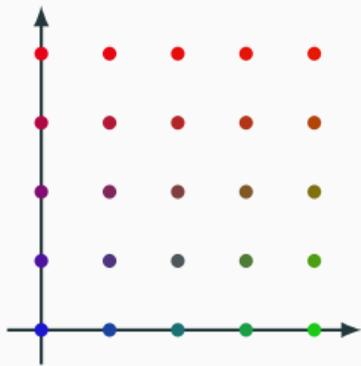


Each pixel is a **column** in our dataset!
We observe **millions to billions of variables**
on cohorts of **a few thousand patients**.

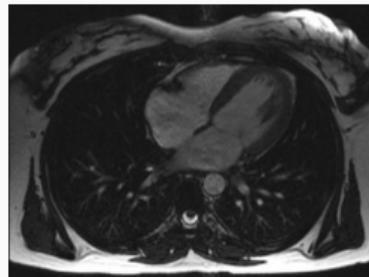
Sampling the full space of medical images is impossible



1 number
→ 5 samples



2 numbers
→ 5^2 samples

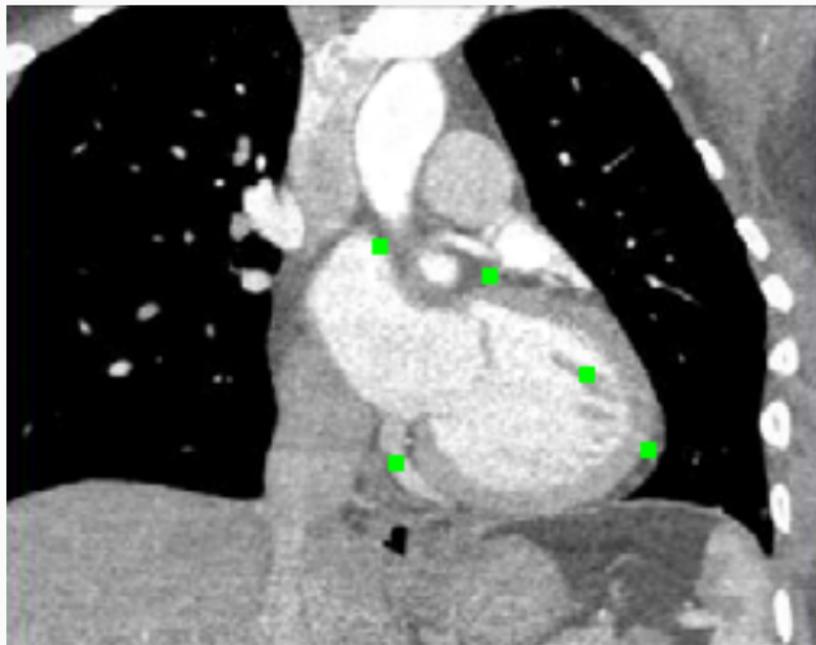


128 · 128 numbers
→ $5^{128 \cdot 128}$ samples

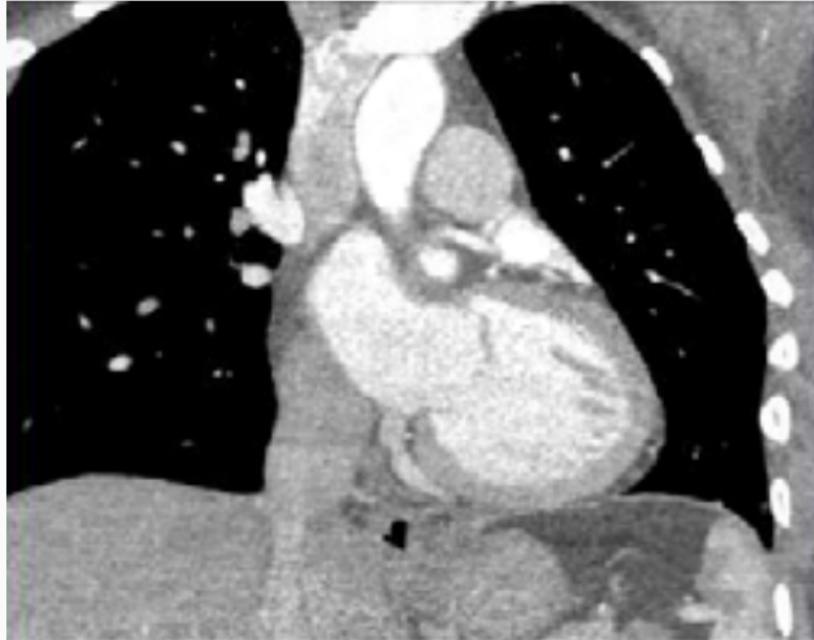
The set of all 2D/3D images is **way too large**
to be sampled with a satisfying accuracy.

First remark: we cannot rely on sparsity

A good radiology exam does not rely exclusively on **5 or 10 pixels**.
We must learn how to **group pixels** in relevant bundles.

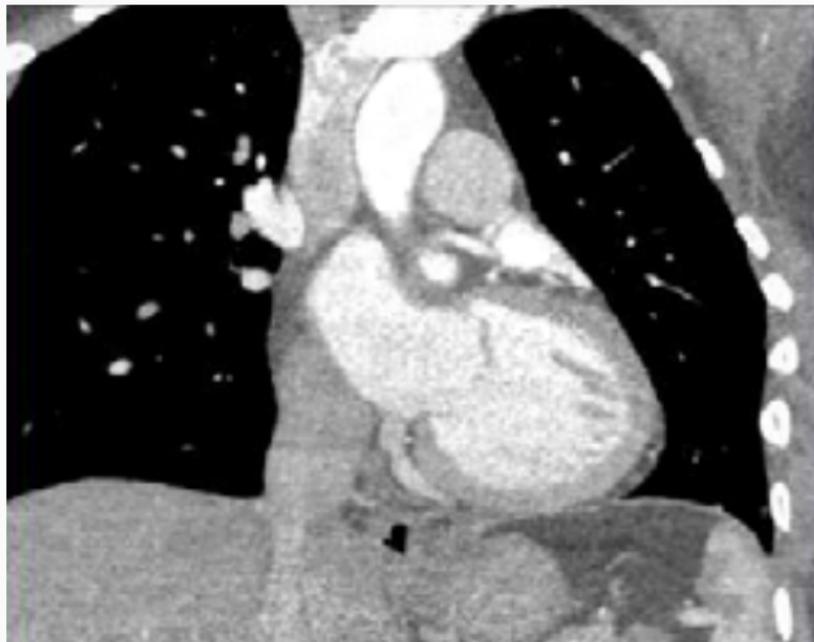


What do you see on a chest image? [EPW11, Man11]



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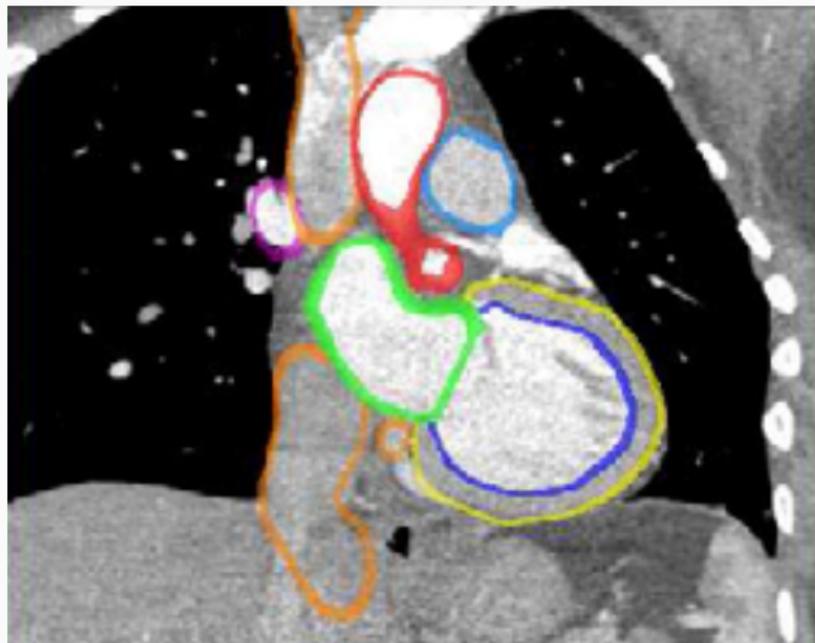
1. Pixels



What do you see on a chest image? [EPW11, Man11]

1. Pixels

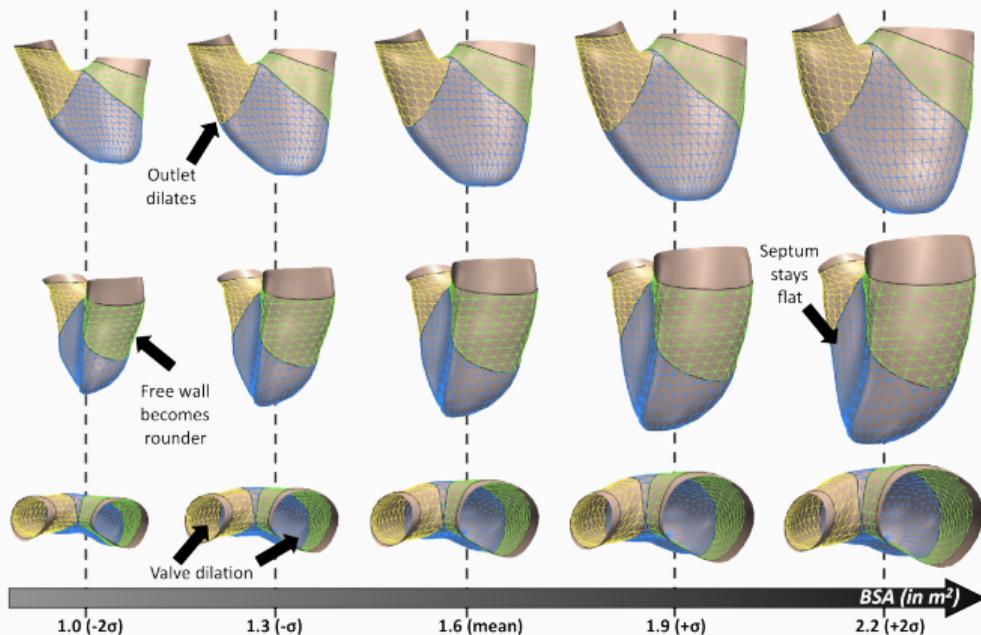
2. Anatomy



What do you see on a chest image? [EPW11, Man11]

1. Pixels

2. Anatomy

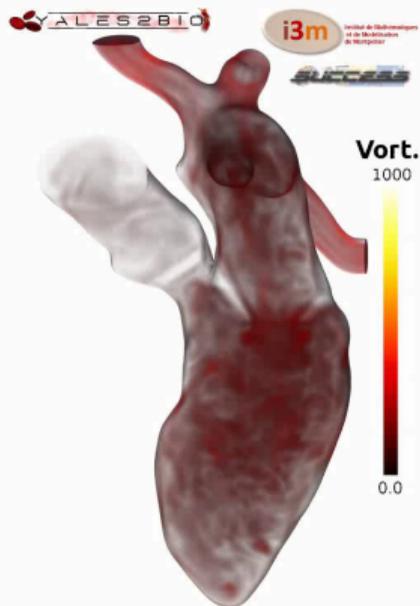


What do you see on a chest image? [EPW11, Man11]

1. Pixels

2. Anatomy

3. Function



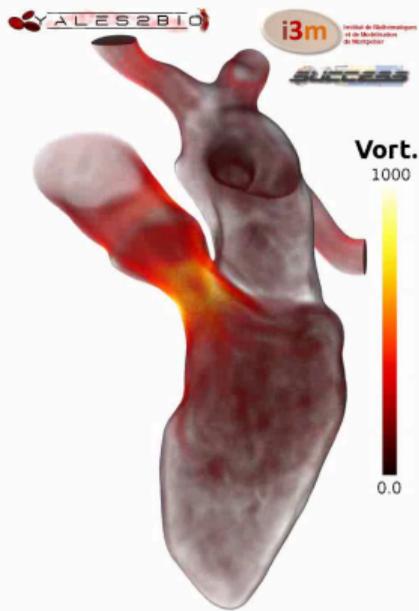
Time: 0 ms

What do you see on a chest image? [EPW11, Man11]

1. Pixels

2. Anatomy

3. Function



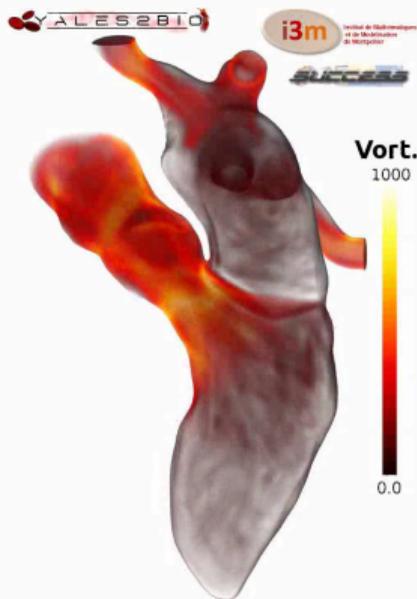
Time: 100 ms

What do you see on a chest image? [EPW11, Man11]

1. Pixels

2. Anatomy

3. Function



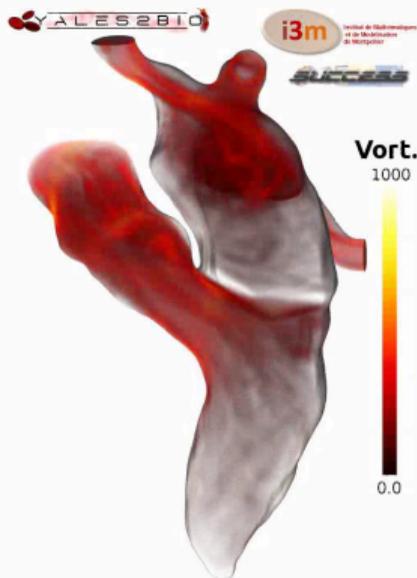
Time: 200 ms

What do you see on a chest image? [EPW11, Man11]

1. Pixels

2. Anatomy

3. Function



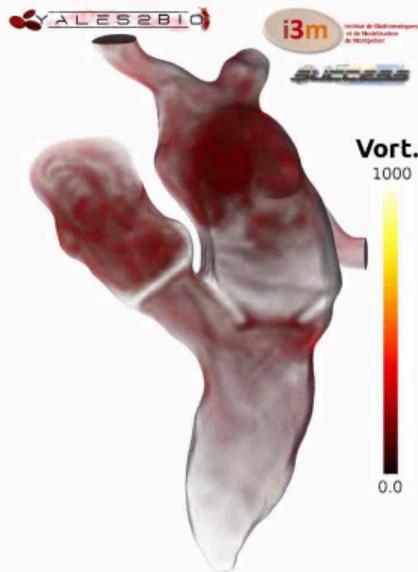
Time: 300 ms

What do you see on a chest image? [EPW11, Man11]

1. Pixels

2. Anatomy

3. Function



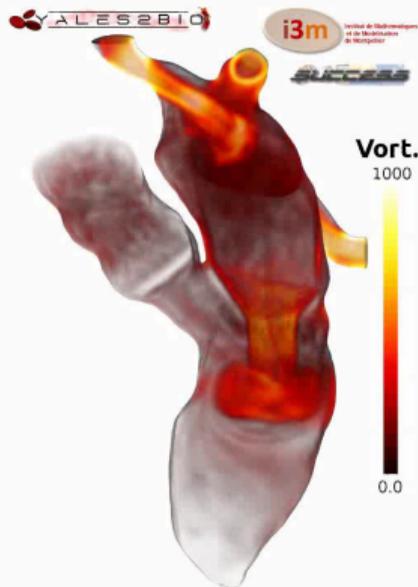
Time: 400 ms

What do you see on a chest image? [EPW11, Man11]

1. Pixels

2. Anatomy

3. Function



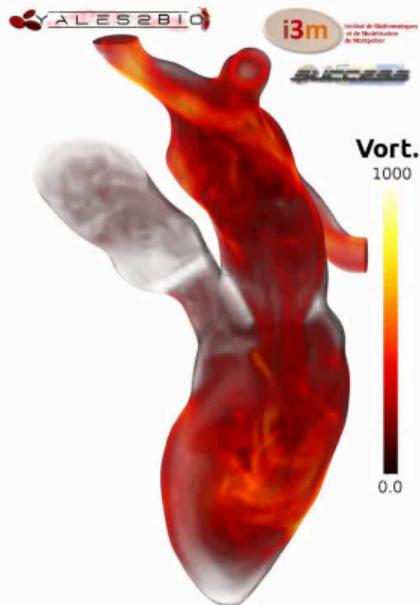
Time: 500 ms

What do you see on a chest image? [EPW11, Man11]

1. Pixels

2. Anatomy

3. Function



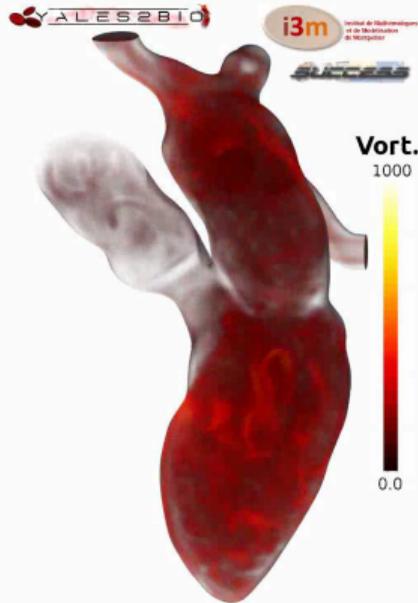
Time: 600 ms

What do you see on a chest image? [EPW11, Man11]

1. Pixels

2. Anatomy

3. Function



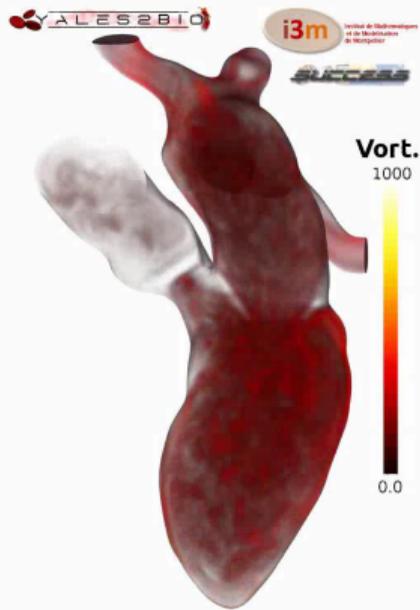
Time: 700 ms

What do you see on a chest image? [EPW11, Man11]

1. Pixels

2. Anatomy

3. Function



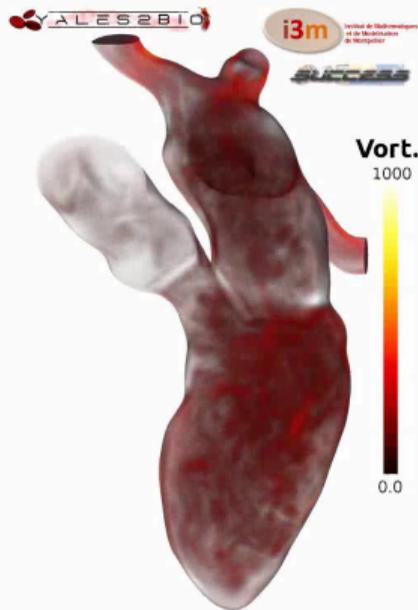
Time: 800 ms

What do you see on a chest image? [EPW11, Man11]

1. Pixels

2. Anatomy

3. Function



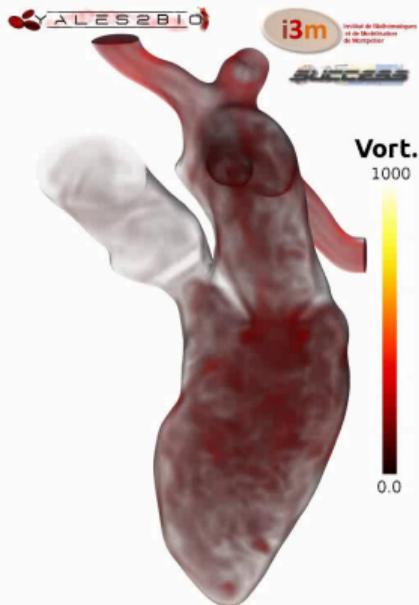
Time: 900 ms

What do you see on a chest image? [EPW11, Man11]

1. Pixels

2. Anatomy

3. Function



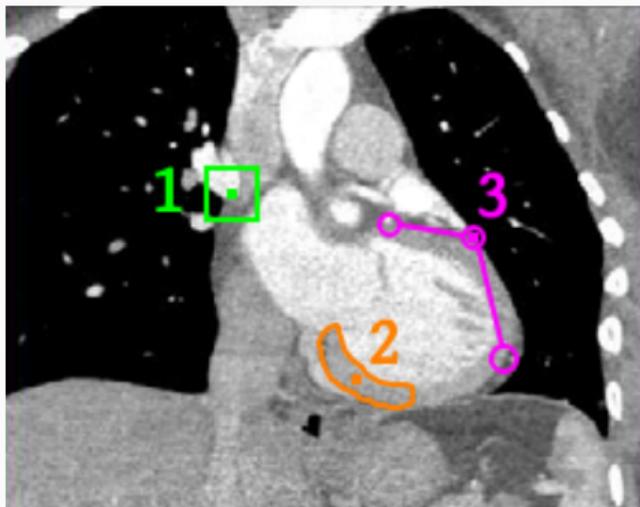
Time: 0 ms

What do you see on a chest image? [EPW11, Man11]

1. Pixels

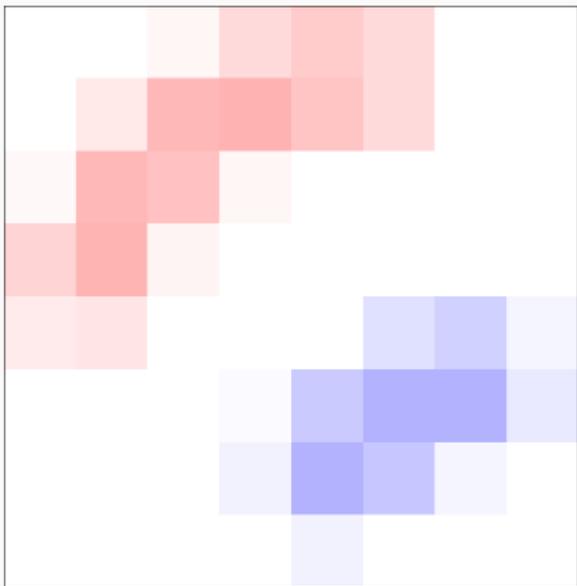
2. Anatomy

3. Function



Simplifying a bit, each level of analysis corresponds to a way of **grouping pixels** with their neighbors.

1st level: a pixel grid

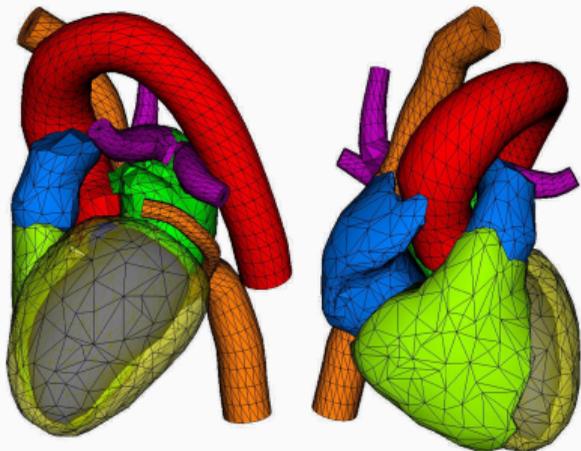


$N_x \times N_y \times N_z$ array of pixels.

Bitmap images and volumes:

- .bmp, .png, .jpg
 - Standard in **radiology**.
-
- + Ordered memory structure.
 - + Explicit neighborhoods.
 - + Fast **convolutions**.
-
- **Texture** analysis.
 - Organ **segmentation**.
 - Pattern **detection**.

2nd level: point clouds and 3D surfaces [EPW11]

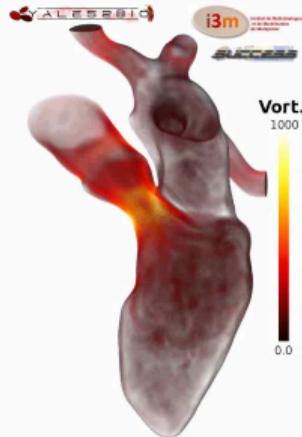


$N_{\text{points}} \times 3$ array of (x, y, z) coordinates.

Clouds of points (\pm triangles):

- .svg
 - Standard for **video games**.
- + Compact representation.
+ High precision geometry.
+ **Easy to deform**.
- **3D visualization**.
→ Anatomical **atlas**.
→ **Shape** analysis.

3rd level: biomechanical and/or physiological model [Man11]



Time: 100 ms

Volumetric mesh,
graph of interactions.

Mechanical/biological model:

- Finite elements, networks.
 - Standard for **CAD**.
-
- + Prior **knowledge**.
 - + **Robust** to noise.
 - + **Realistic** behaviour.
-
- **Physiological** interpretation.
 - **Infer** what cannot be seen (blood flow).
 - **Simulate** a surgery.

To summarize

We must combine a **statistical regression** method with a **relevant model**.

In medical imaging, we may work with:

1. A 2D or 3D **pixel grid**.
2. An array of (x, y, z) **coordinates**.
3. A **web** of complex interactions.
4. Everything at once!

In most cases, we will define a large **structured formula**:

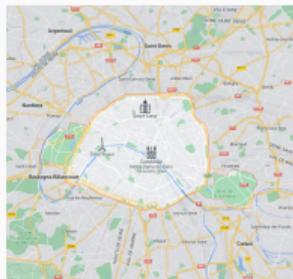
$$\text{image} \xrightarrow{\mathbf{F}} \mathbf{F}(\text{image}) \simeq \text{diagnostic}$$

F is a parametric computing **architecture**
 \simeq **model** to fit \simeq **network** to train.

2. How can I choose a good model?

A model is like a map: a warped and partial view of the world [Duk, Str]

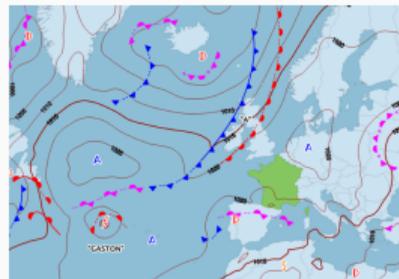
How can I trust these pictures?



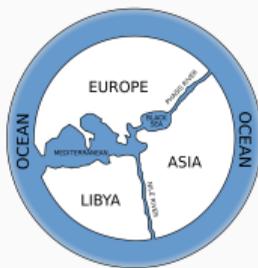
Google



RATP



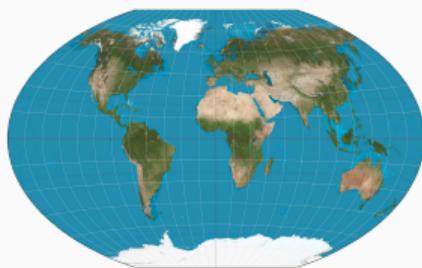
Météo France



Anaximander



Mercator



Winkel

The map is not the territory

A map is not the territory it represents, but, if correct,
it has a **similar structure** to the territory,
which accounts for its **usefulness**.

– Alfred Korzybski, 1933.

On exactitude in science – Jorge Luis Borges, 1946, translated by Andrew Hurley.

...In that empire, the art of cartography attained such **perfection** that the map of a single **province** occupied the entirety of a **city**, and the map of the **empire**, the entirety of a **province**. In time, those unconscionable maps no longer satisfied, and the cartographers guilds struck **a map of the empire whose size was that of the empire**, and which coincided point for point with it.

The following generations, who were not so fond of the study of cartography as their forebears had been, saw that **that vast map was useless**, and not without some pitilessness was it, that they delivered it up to the inclemencies of sun and winters. In the **deserts** of the West, still today, there are tattered **ruins of that map**, inhabited by animals and beggars; in all the land there is no other relic of the disciplines of geography.

– Suarez Miranda, *Viajes de varones prudentes*, Libro IV, Cap. XLV, Lerida, 1658

What is a good model?

A good map should:

- **Highlight** the relevant key points and roads.
This is a **task-specific** objective (car, bike...).
- **Hide** unnecessary information to reduce clutter: **the lighter, the better**.
Heavy maps *will* be discarded by the next generation.
- Be **accurate** – up to a required **tolerance**.
There is a **tradeoff** here: think of the metro map!
- Be **transparent** about **omissions and distortions**.
This is the main **trap** that we should not forget.

What is a good model?

All these points apply to ML models:

- **Highlight** the stuff that matters.
- **Discard** the rest.
- Be **accurate** – up to a sensible tolerance.
- Be **transparent** and **honest**.

Of course, raw “performance” results do matter: **accuracy** is a real thing.

But most importantly, a good model should be **legible** and enable **creativity**.

Example 1: The sphere of triangles

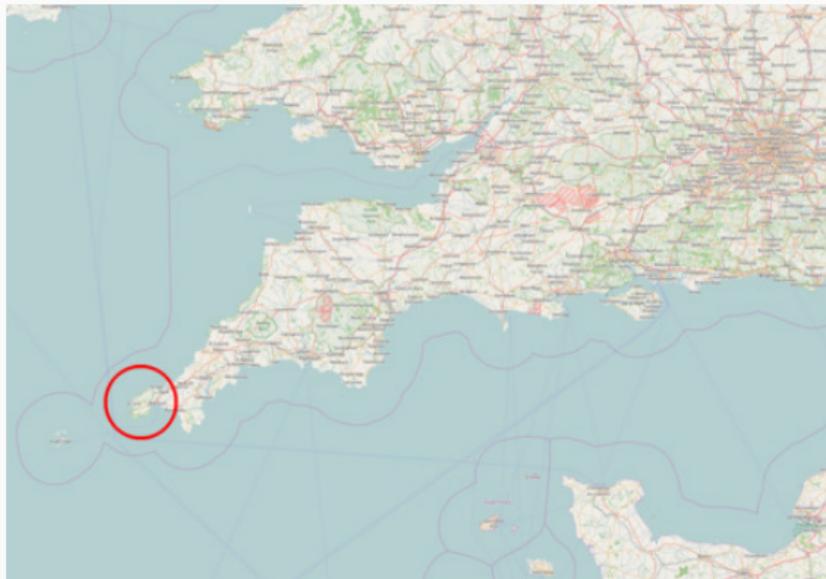
Surprisingly enough, our story starts with... Menhirs!



More precisely: with the distribution of megaliths in the Land's End peninsula



52 Menhir locations.



Cornwall, in South-West England.

Can you see **alignments** here? Some people do.

Many authors have claimed that these **ley lines** demarcate “Earth energies” and/or serve as guides for alien spacecraft.

Understanding triangle shapes

Back in 1974, this problem motivated David Kendall to ask a question:

Assuming that I draw 52 points at random in a square...

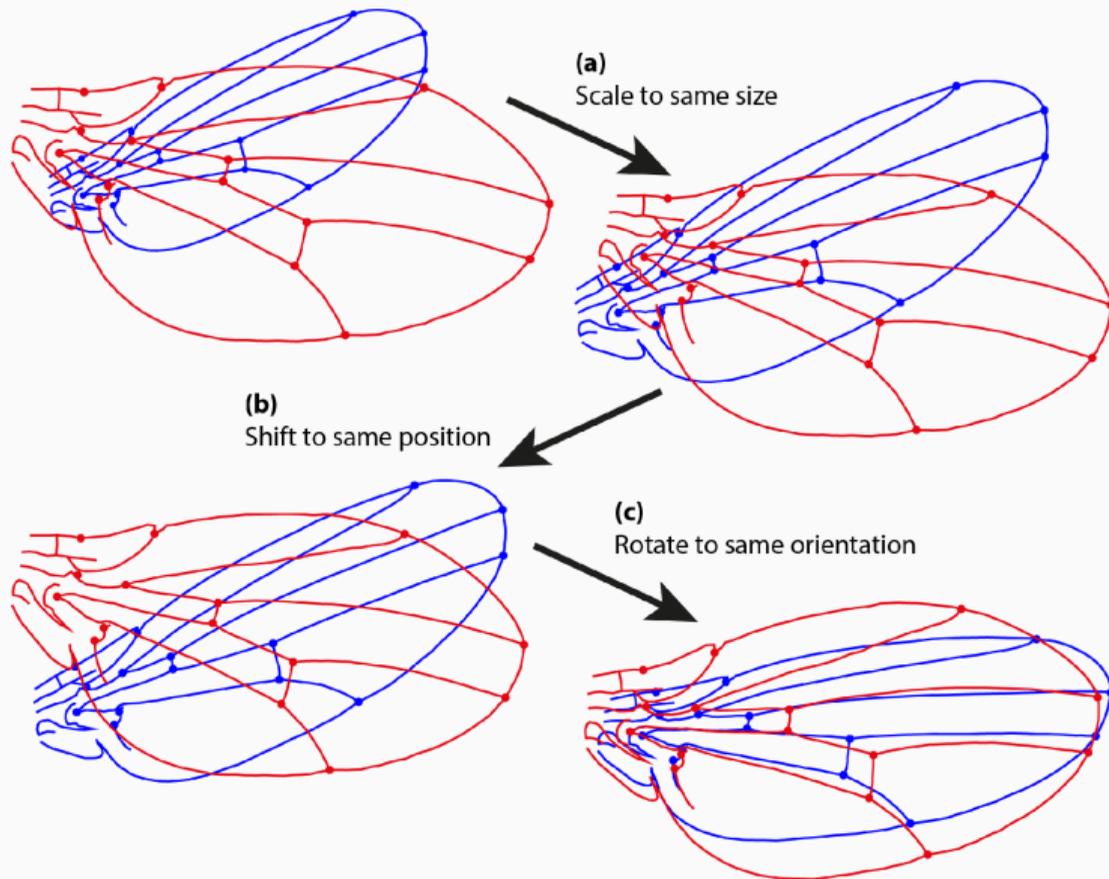
How many **flat triangles** (say, with a $180^\circ \pm 1^\circ$ angle) am I going to observe?

This prompted a remarkable series of papers:

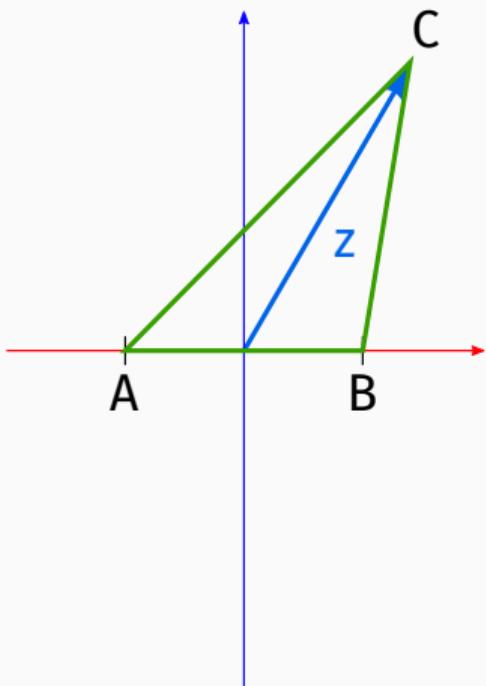
- *The diffusion of shape*, Kendall, 1977.
- *Alignments in two-dimensional **random sets of points***, Kendall and Kendall, 1980.
- *Simulating the **ley hunter***, Broadbent, 1980.
- *Shape manifolds, Procrustean metrics, and complex projective spaces*, Kendall, 1984.

And the the birth of modern shape analysis.

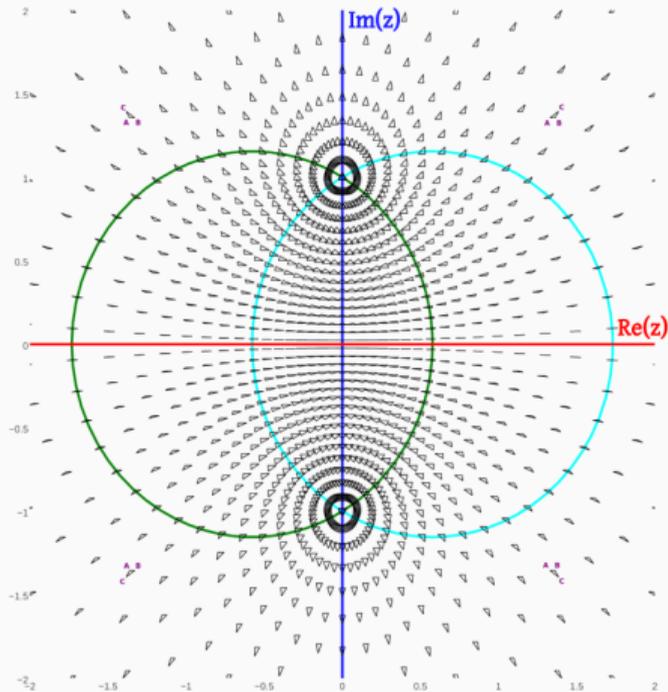
Step 1: Working with shapes up to similarities [Kli15]



Step 2: The space of triangles up to similarities is two-dimensional

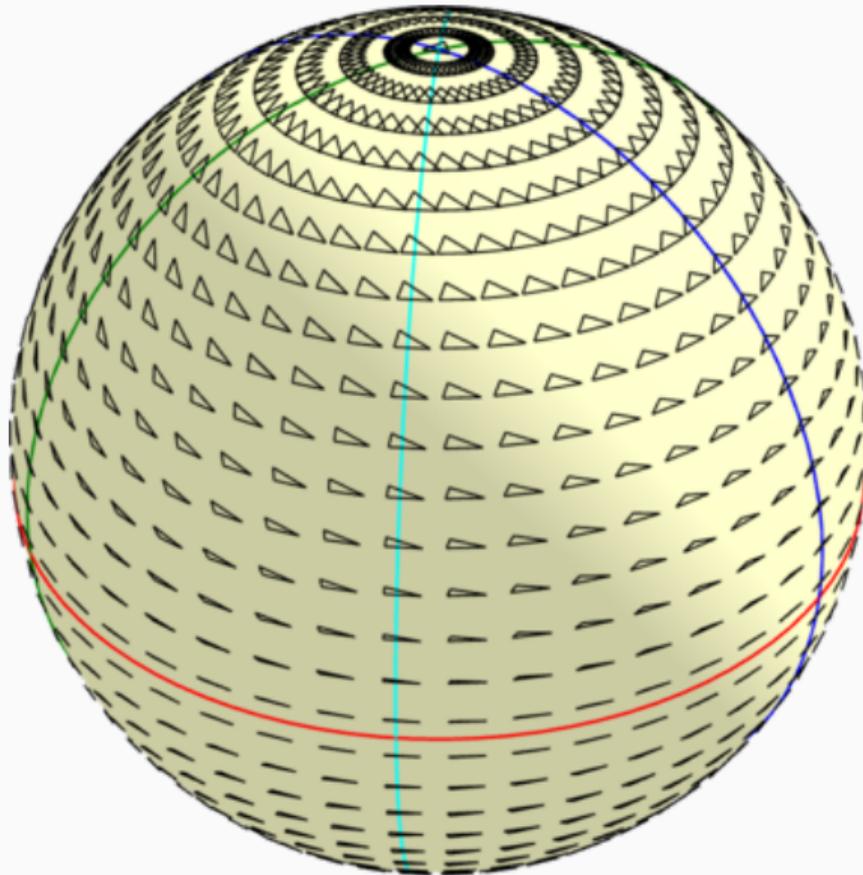


Send A to $(-1, 0)$
and B to $(+1, 0)$.

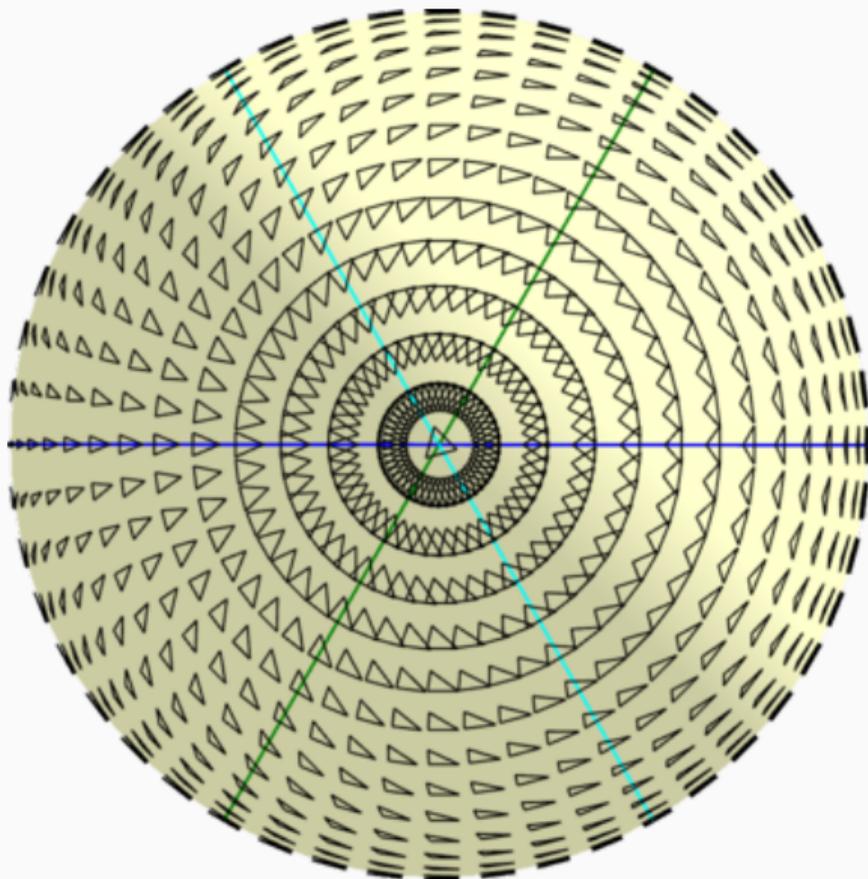


Identify $z \in \mathbb{C} \cup \{\infty\}$
with all non-degenerate triangle shapes.

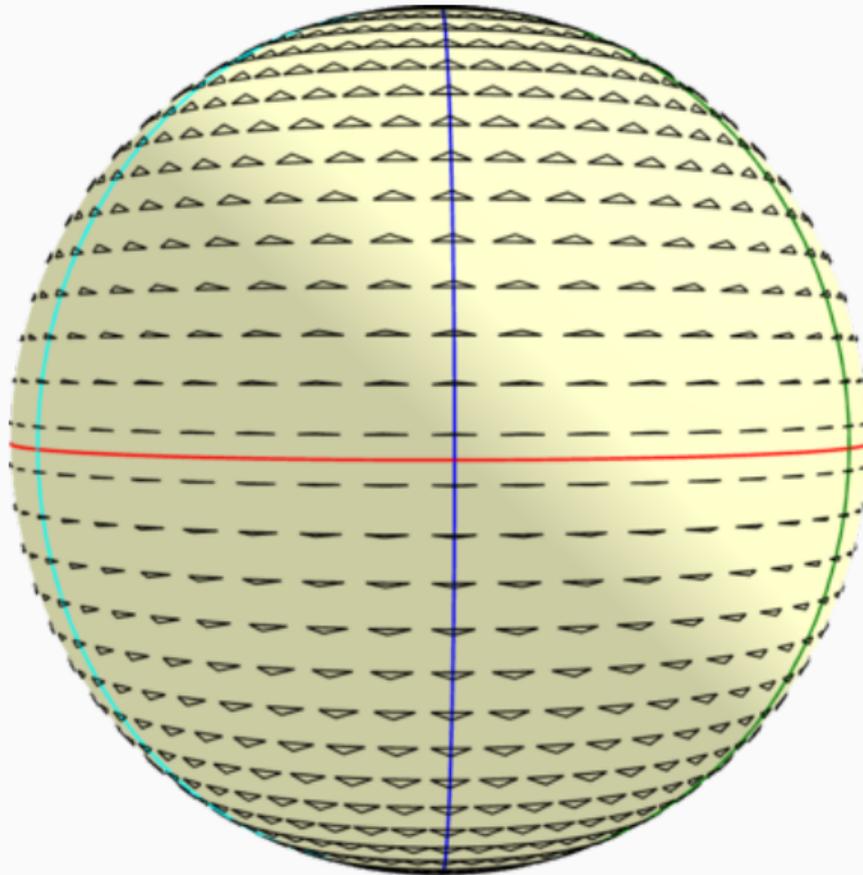
Step 3: Up to a clever change of coordinates: this is actually a sphere!



The two poles correspond to the direct and indirect equilateral triangles



The Equator corresponds to the set of flat triangles



First properties of this map

This representation respects the main **symmetries** of the set of triangles:

- The sets of **isocetes triangles** with respect to A, B and C correspond to three **great circles** that are equally spaced with each other.
- **Axial symmetries** correspond to a North-South inversion across the Equator.
- The Equator of flat triangles + the meridians of isocetes triangles cut the sphere in **12 pieces**. These exactly correspond to the 6 permutations of the vertices $ABC \times \{ \text{the identity or an axial symmetry} \}$.

But there is more!

Metric properties of the spherical embedding

$$\mathbf{K} : (A, B, C) \in \mathbb{R}^{3 \times 2} \setminus \{A = B = C\} \mapsto \mathbf{K}(A, B, C) \in \mathbb{R}^3$$

denotes the **Kendall embedding** from the set of non-degenerate triangles to the sphere of center $(0, 0, 0)$ and diameter 1.

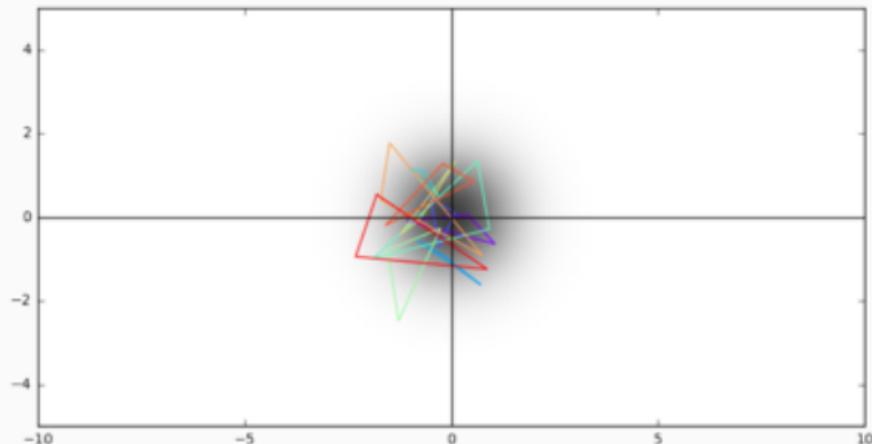
(It has an OK-ish expression using cos and sin.)

Then, straightforward computations show that:

$$\min_{\text{similarity } S} \|S(A) - D\|_{\mathbb{R}^2}^2 + \|S(B) - E\|_{\mathbb{R}^2}^2 + \|S(C) - F\|_{\mathbb{R}^2}^2 = \text{Var}(D, E, F) \cdot \|\mathbf{K}(A, B, C) - \mathbf{K}(D, E, F)\|_{\mathbb{R}^3}^2$$

The **chord distance on the sphere** of Kendall corresponds to the **Euclidean distance** on triplets of points in the plane, **up to similarities**.

Statistical properties of the spherical embedding

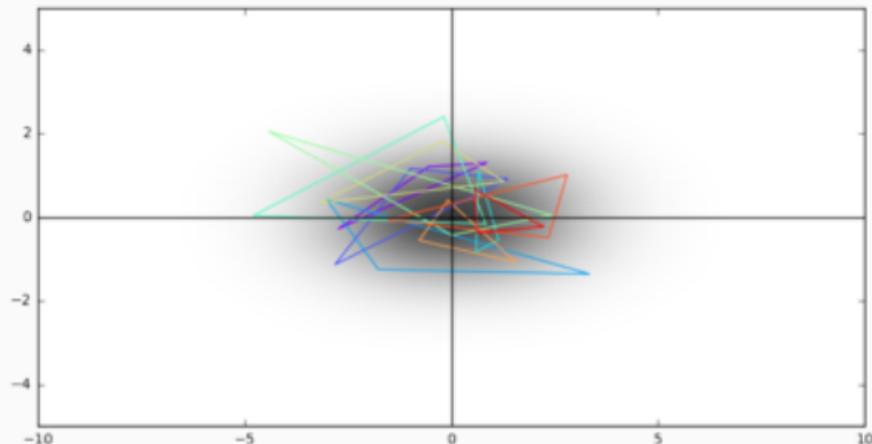


A, B, C are drawn according to an **isotropic** Gaussian distribution on the plane.

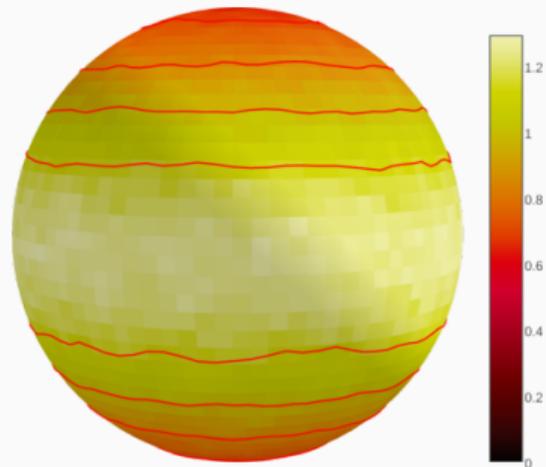


Empirical histogram on the sphere of triangle shapes.

Statistical properties of the spherical embedding

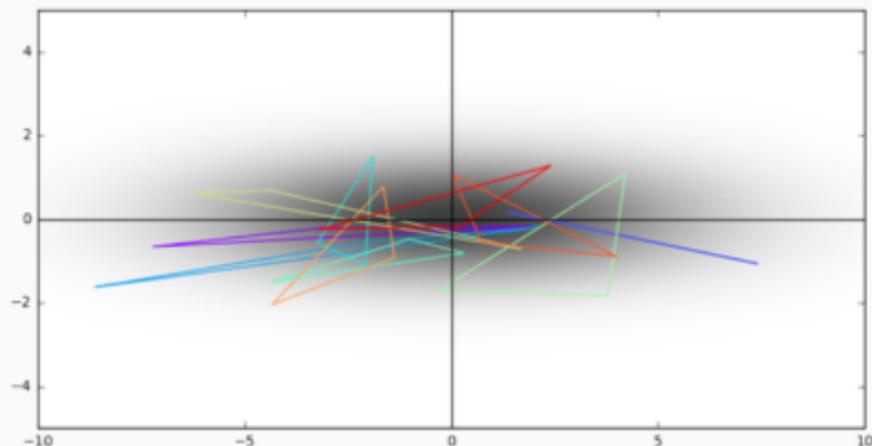


A, B, C are drawn according to a **non-isotropic** Gaussian distribution on the plane.

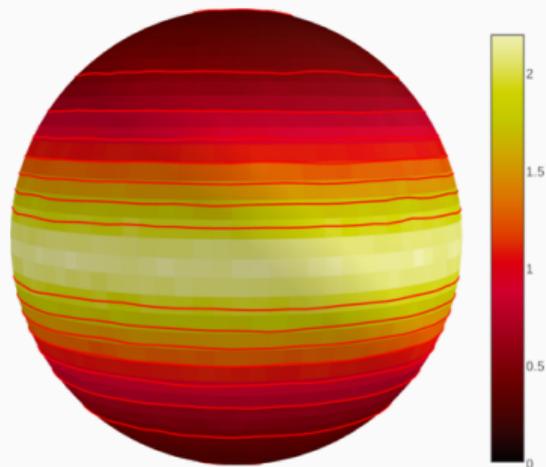


Empirical histogram on the sphere of triangle shapes.

Statistical properties of the spherical embedding



A, B, C are drawn according to a **non-isotropic** Gaussian distribution on the plane.



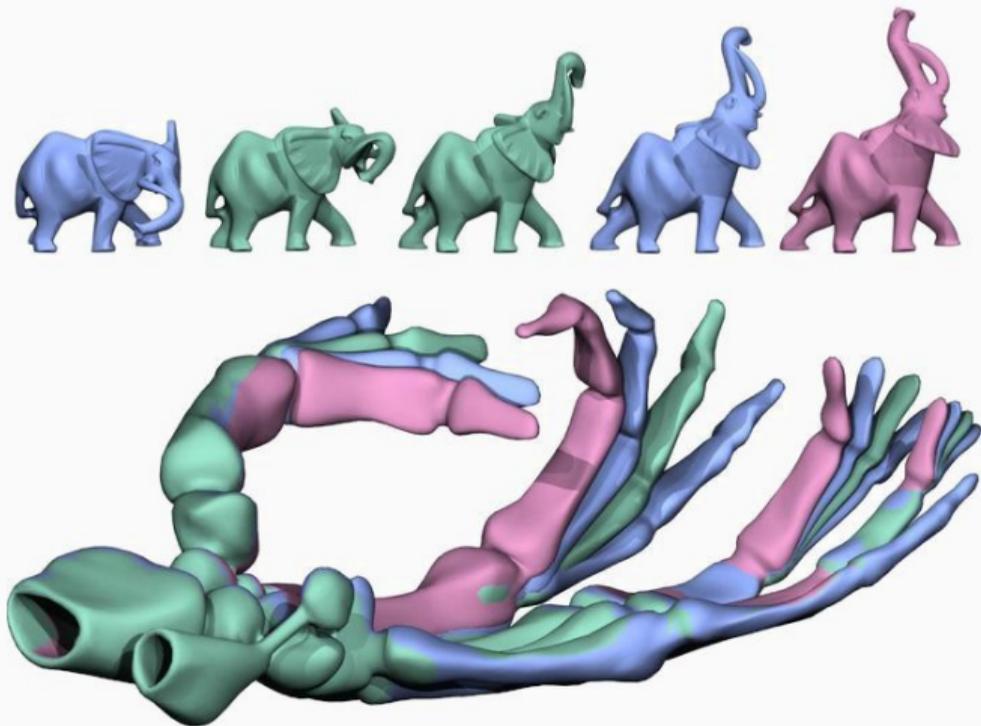
Empirical histogram on the sphere of triangle shapes.

Kendall showed that the space of **triangles** is best understood as a **sphere** for **topological**, **geometric** and **statistical** reasons.

You cannot “unsee” this elegant result.

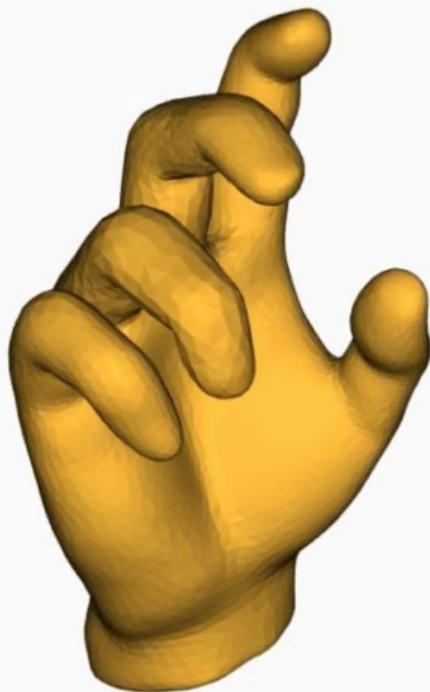
Most importantly, his theorem showed that **shapes** naturally belong to a **curved** geometric space.

This idea is at the heart of modern shape analysis software [KMP07]

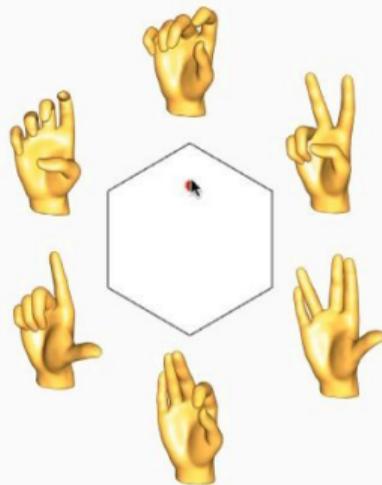


Geodesics in spaces of elephants and skeletons.

This idea is at the heart of modern shape analysis software [vRESH16]



screen captured



Barycentric interpolation in a space of hands.

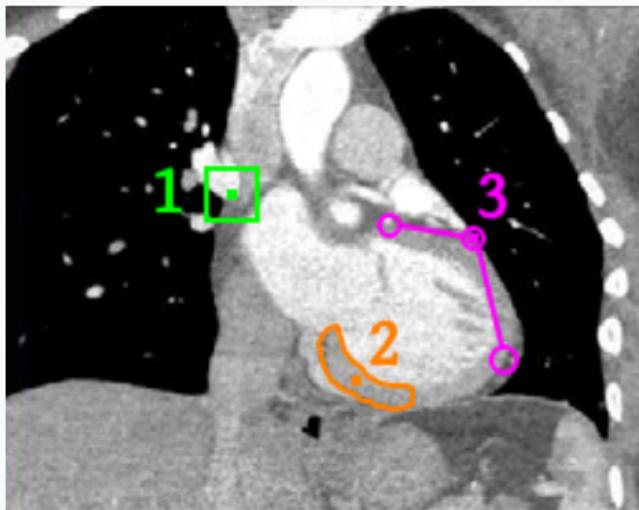
Example 2: Style transfer with convolutional neural networks

Remember that picture? [EPW11]

1. Pixels

2. Anatomy

3. Function



Let's talk about the **first way** of **grouping pixels** with their neighbors.

Filtering, also known as the “convolution product”

Convolution (i.e. weighted average of the neighboring pixels) :

Cheap generalization of the **product** “ $a \cdot x$ ”,
parameterized by the coefficients of a **small filter** φ .



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A multi-scale prior on images

Wavelet theory (1990~2010 ; Meyer, Mallat, Daubechies...) :

Small filters + cascading zoom-out operations [Mal16]:

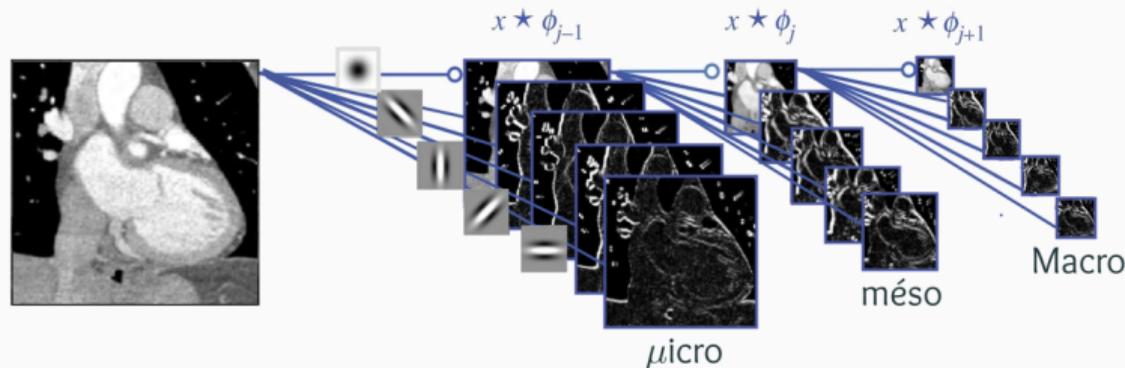
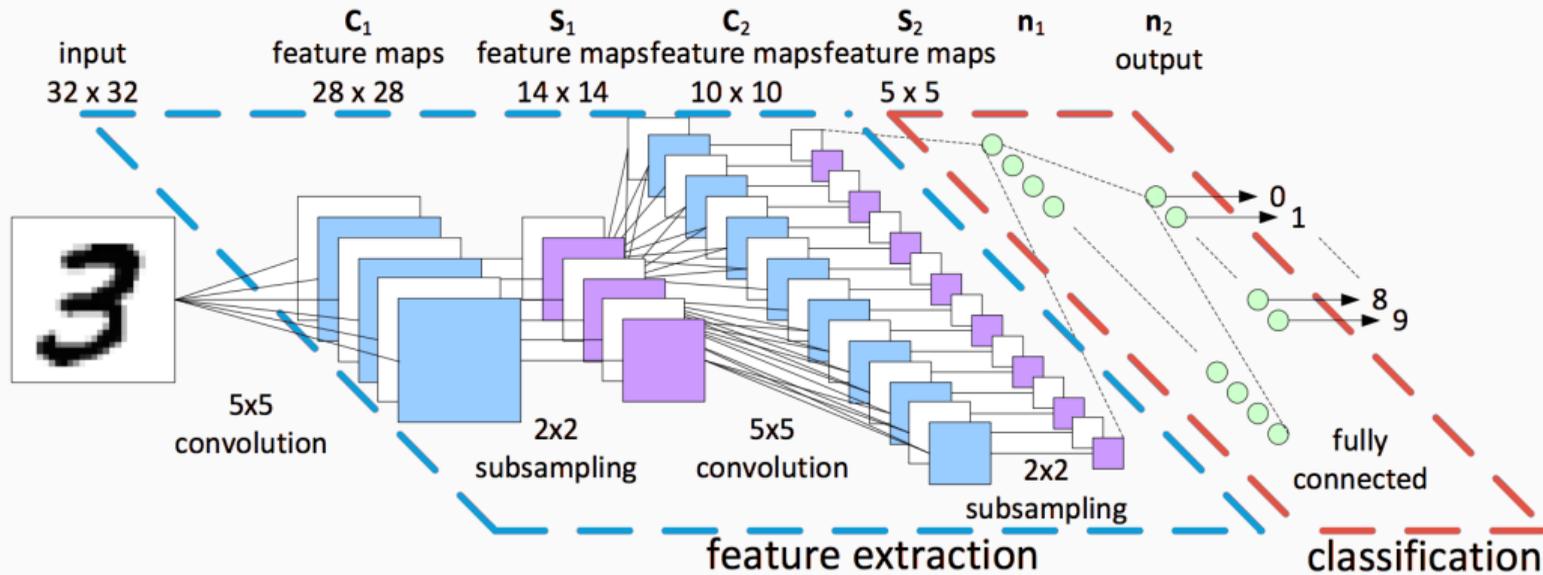


Image \longrightarrow Relevant coefficients
 \simeq “.wav” Audio \longrightarrow Music score

\implies **JPEG2000** format, standard of the movie industry.

Convolutional neural networks [PMC11]

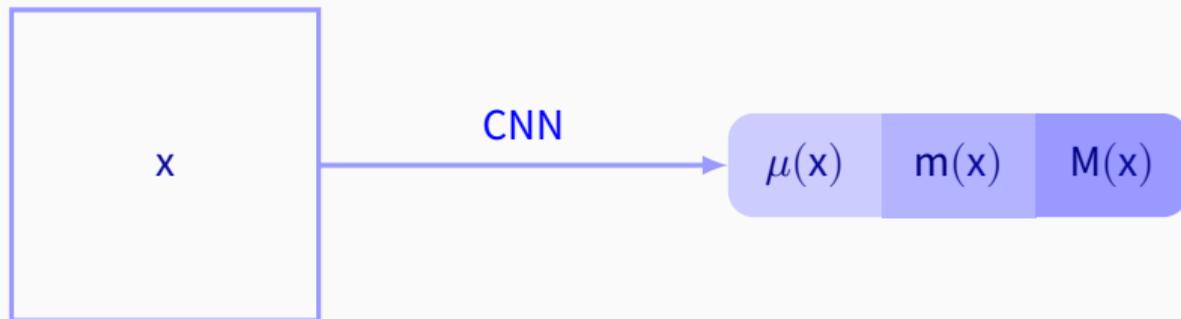


Convolutional Neural Networks as a data-driven “codec” for your data

JPEG2000 relies on a model for natural images that is:

- Computationally cheap.
- Translation-equivariant.
- Encodes a **multi-scale** prior on natural images.

By **tuning its parameters** on a labeled database, we get a **CNN** = domain-specific “JPEG2020”.



An iconic application: Deep Art [NN16]

An iconic application: Deep Art [NN16]



An iconic application: Deep Art [NN16]



An iconic application: Deep Art [NN16]



μ m M

μ m M



An iconic application: Deep Art [NN16]

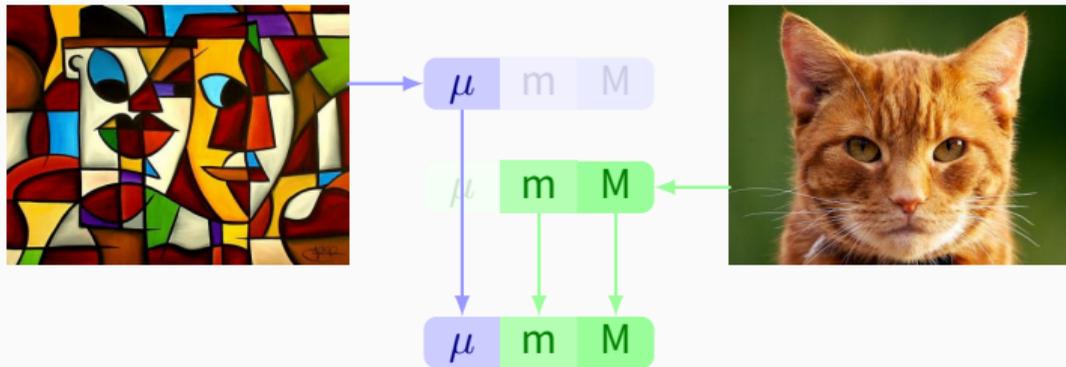


μ m M

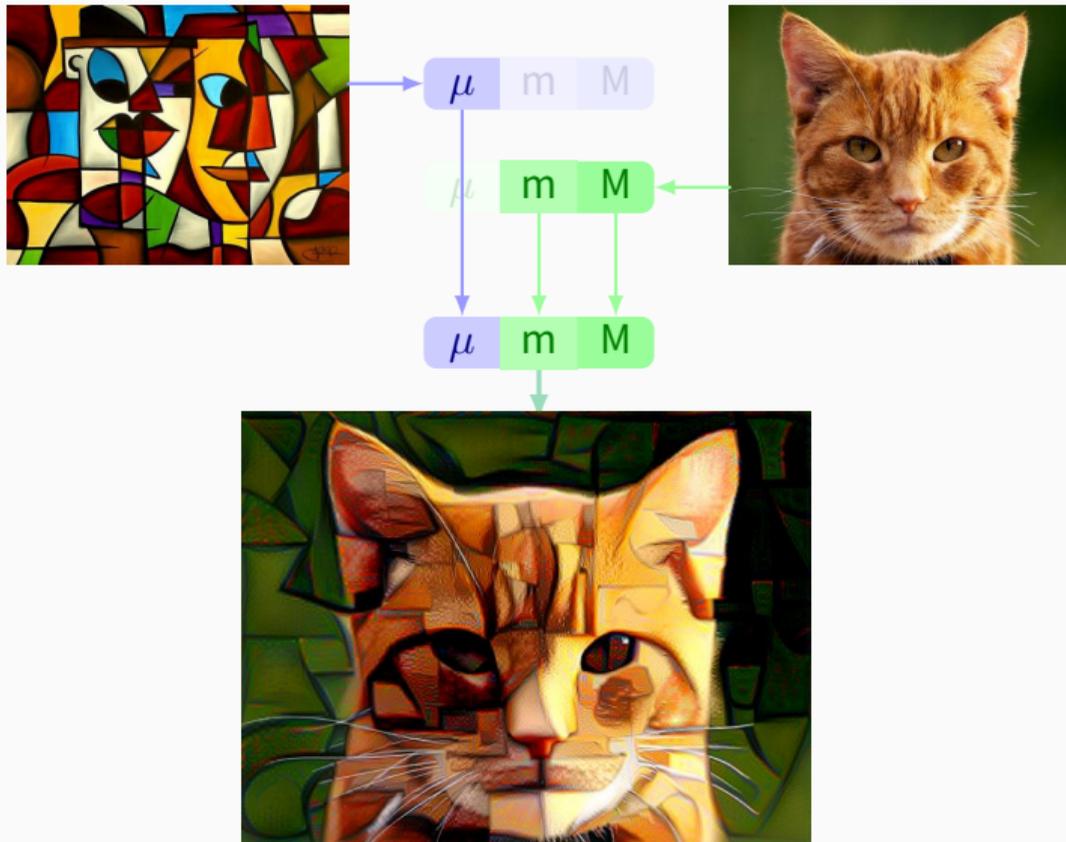
μ m M



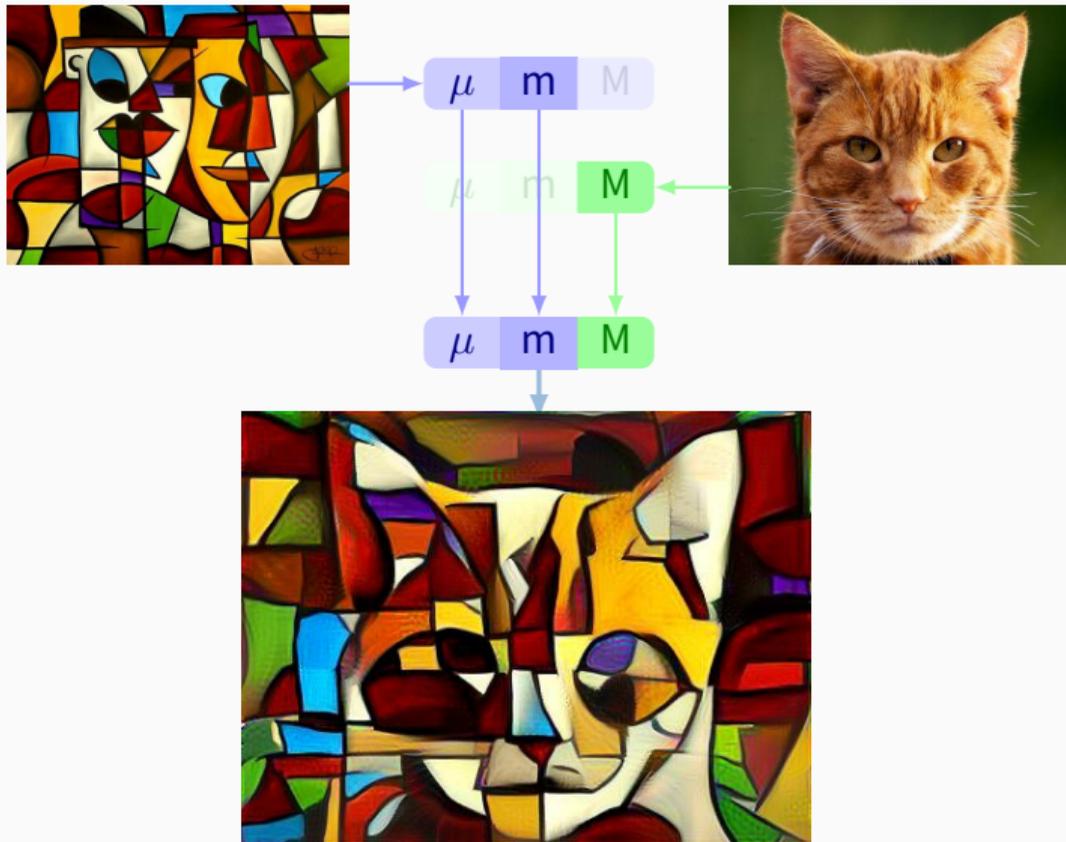
An iconic application: Deep Art [NN16]



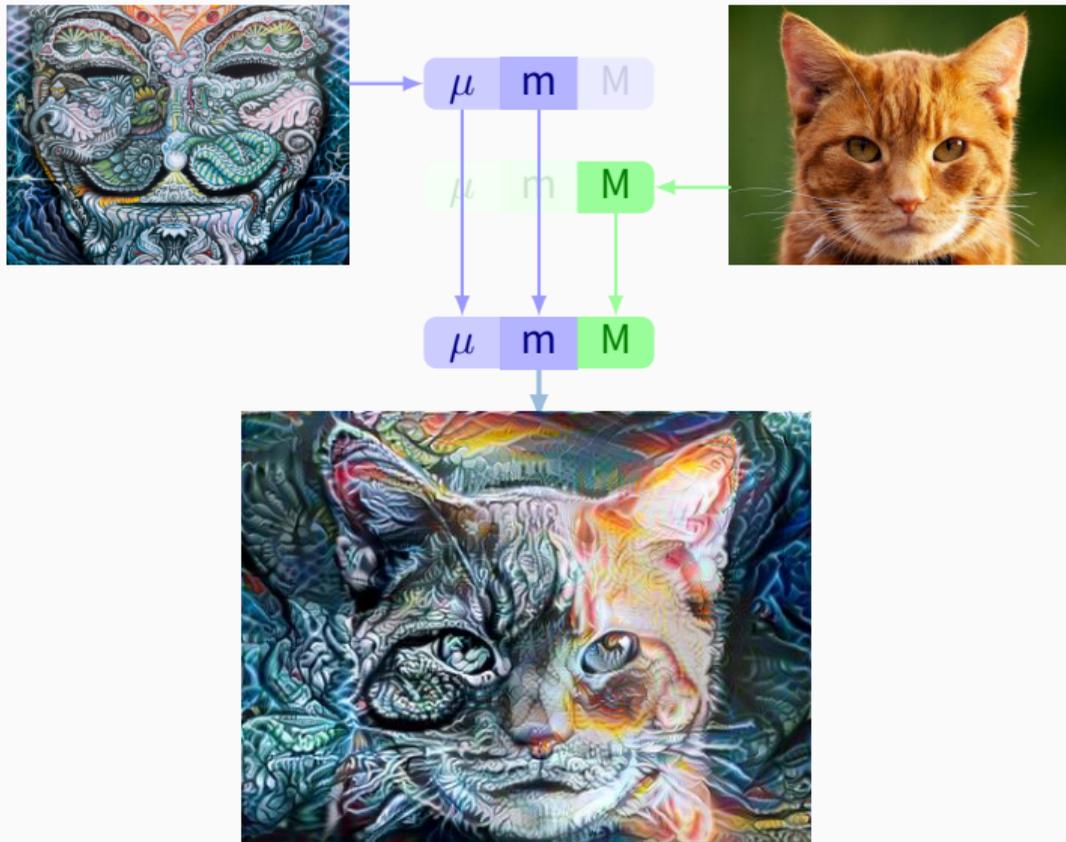
An iconic application: Deep Art [NN16]



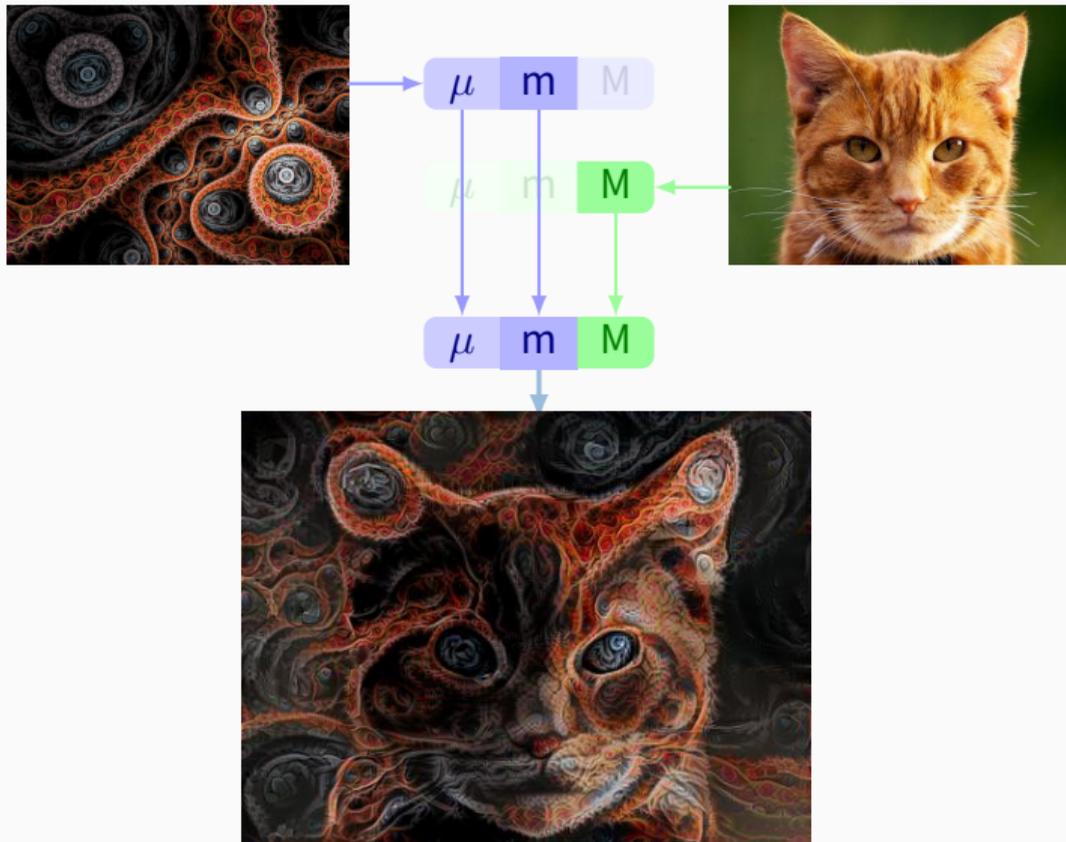
An iconic application: Deep Art [NN16]



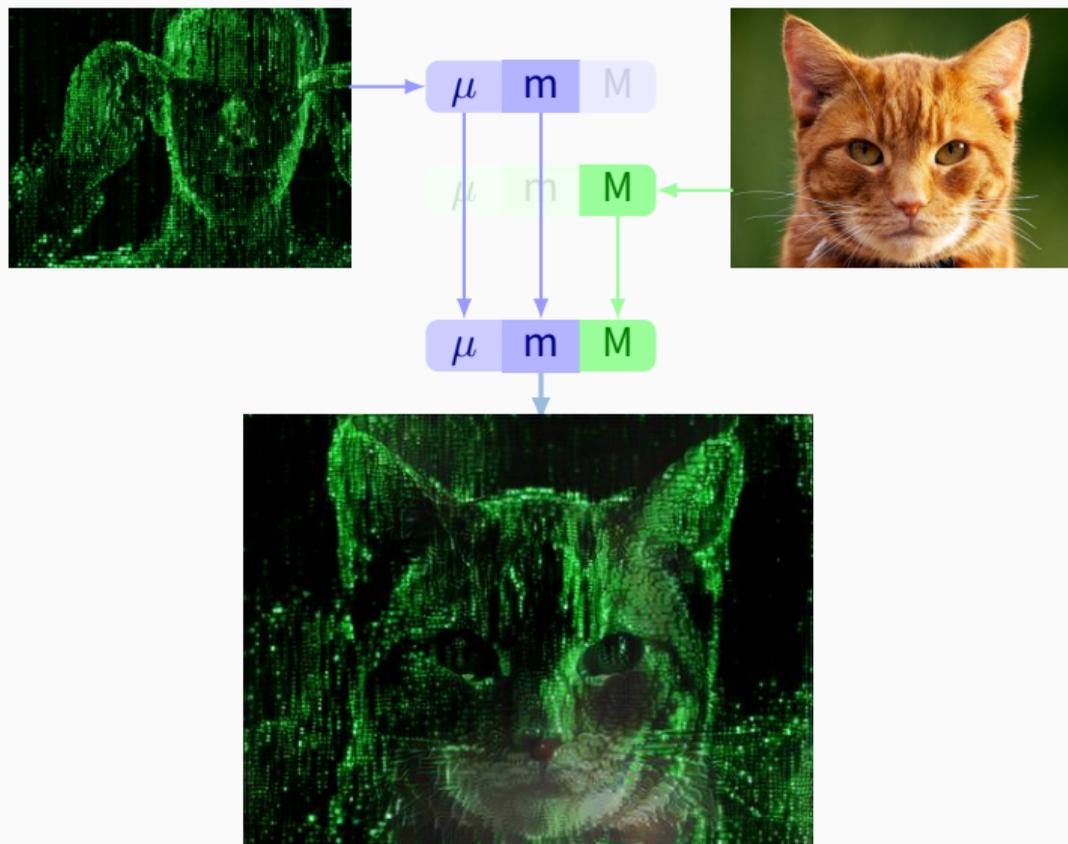
An iconic application: Deep Art [NN16]



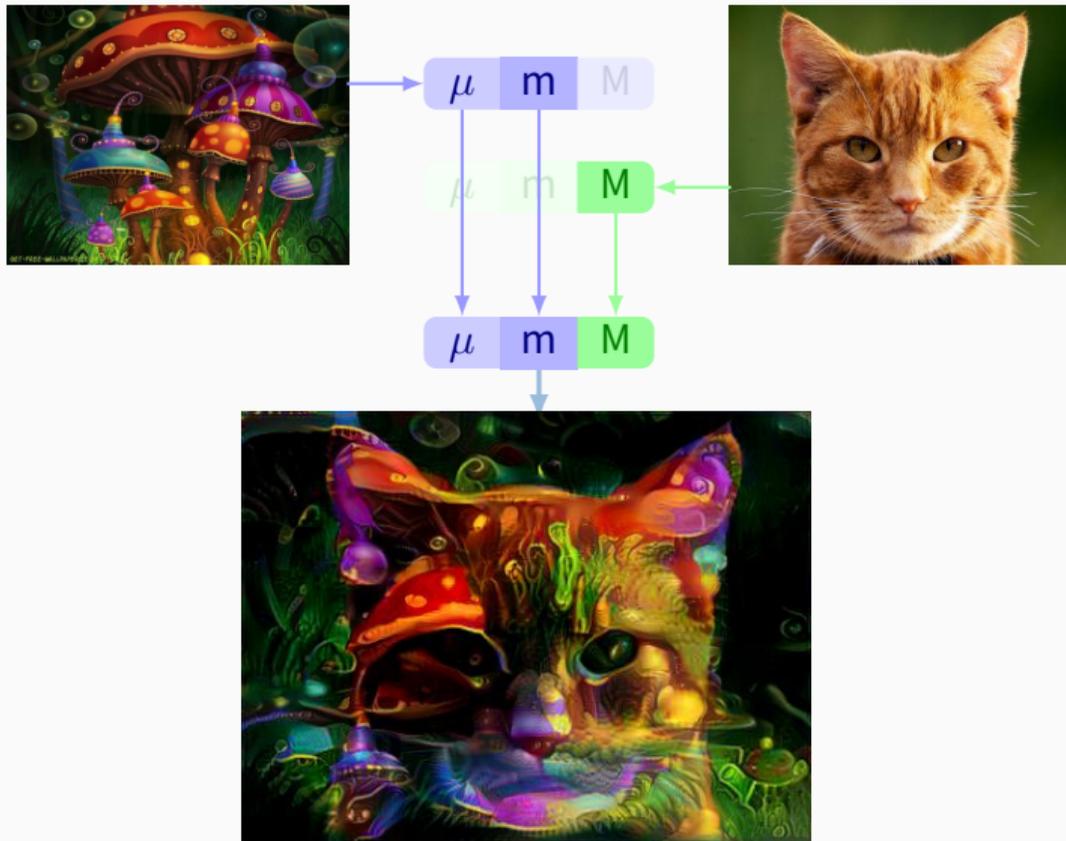
An iconic application: Deep Art [NN16]



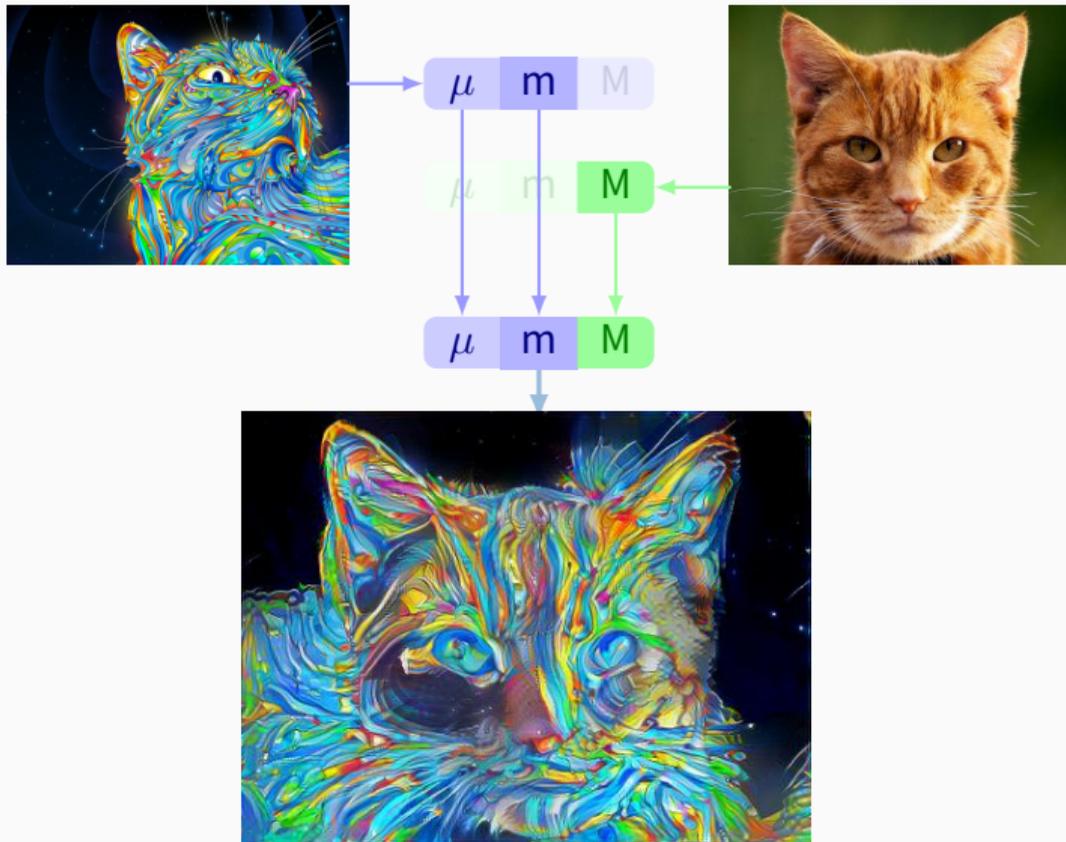
An iconic application: Deep Art [NN16]



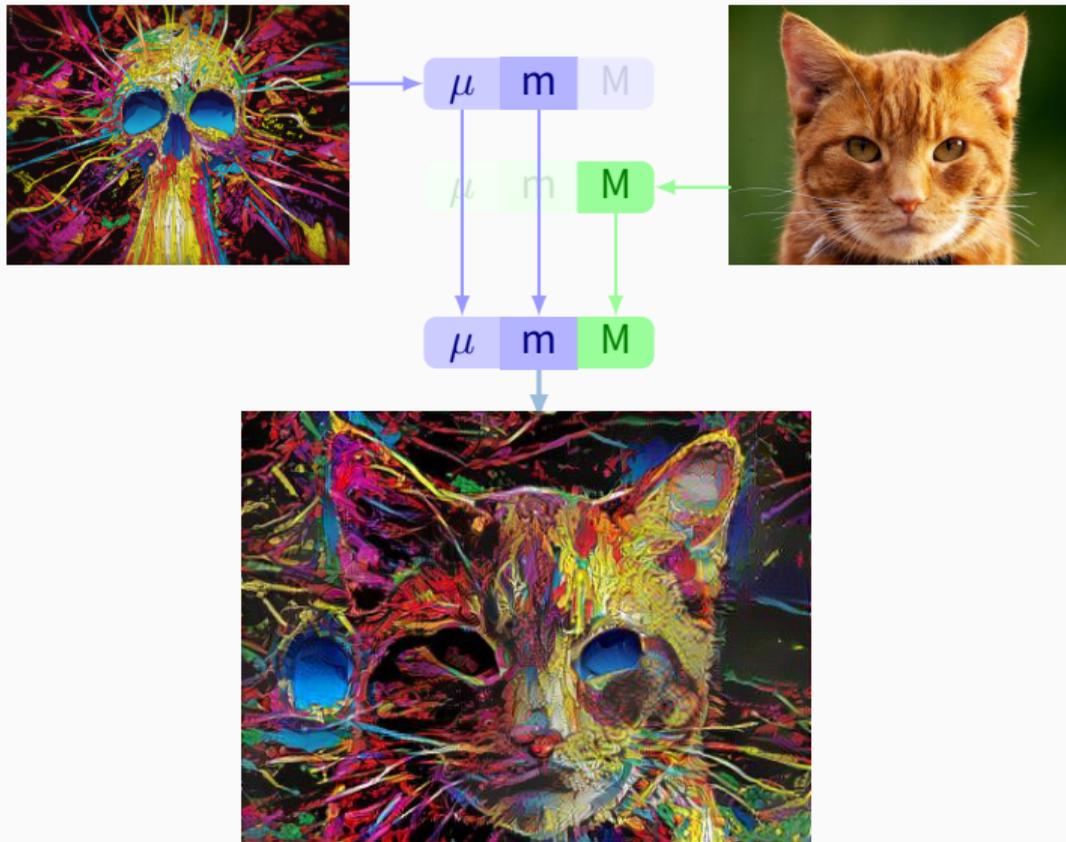
An iconic application: Deep Art [NN16]



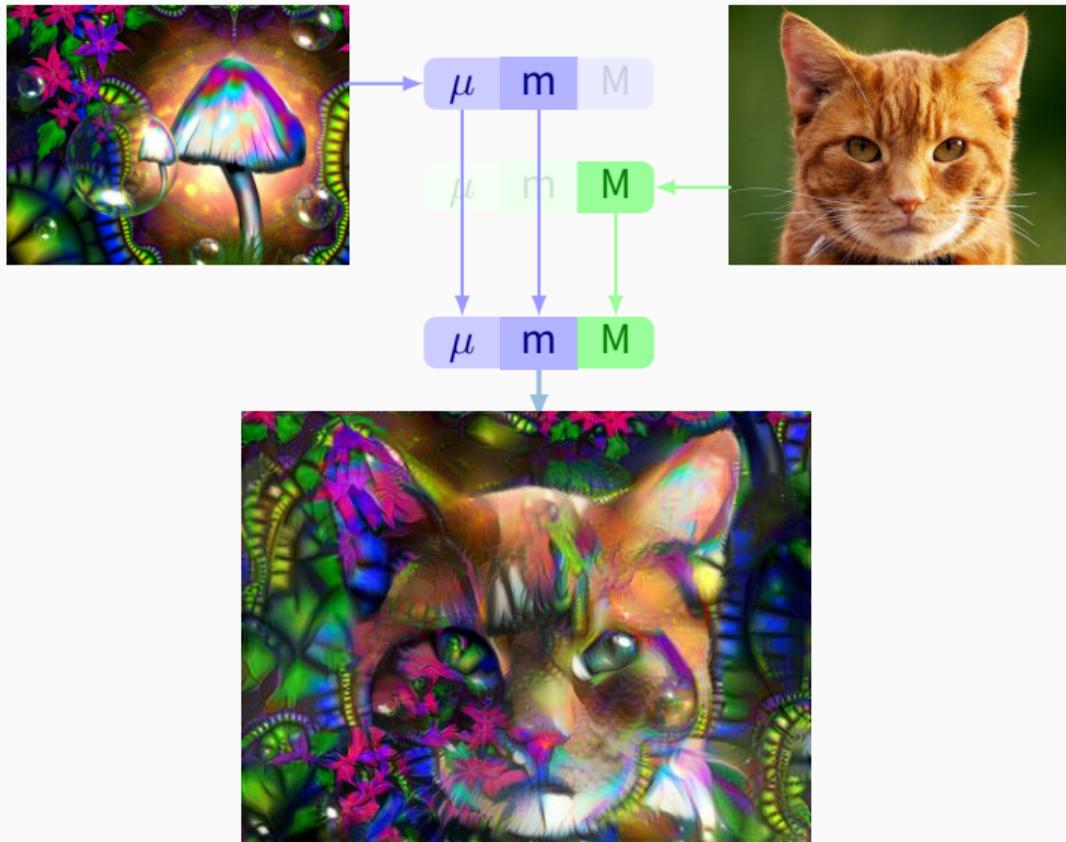
An iconic application: Deep Art [NN16]



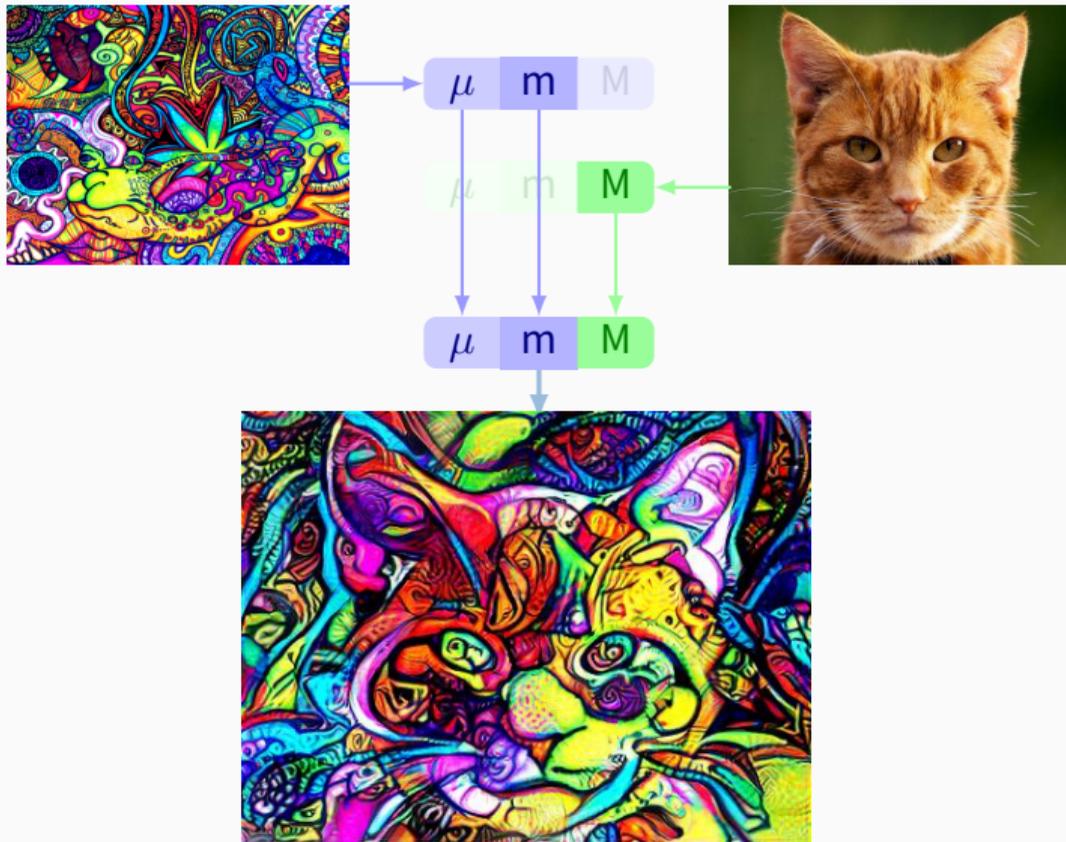
An iconic application: Deep Art [NN16]



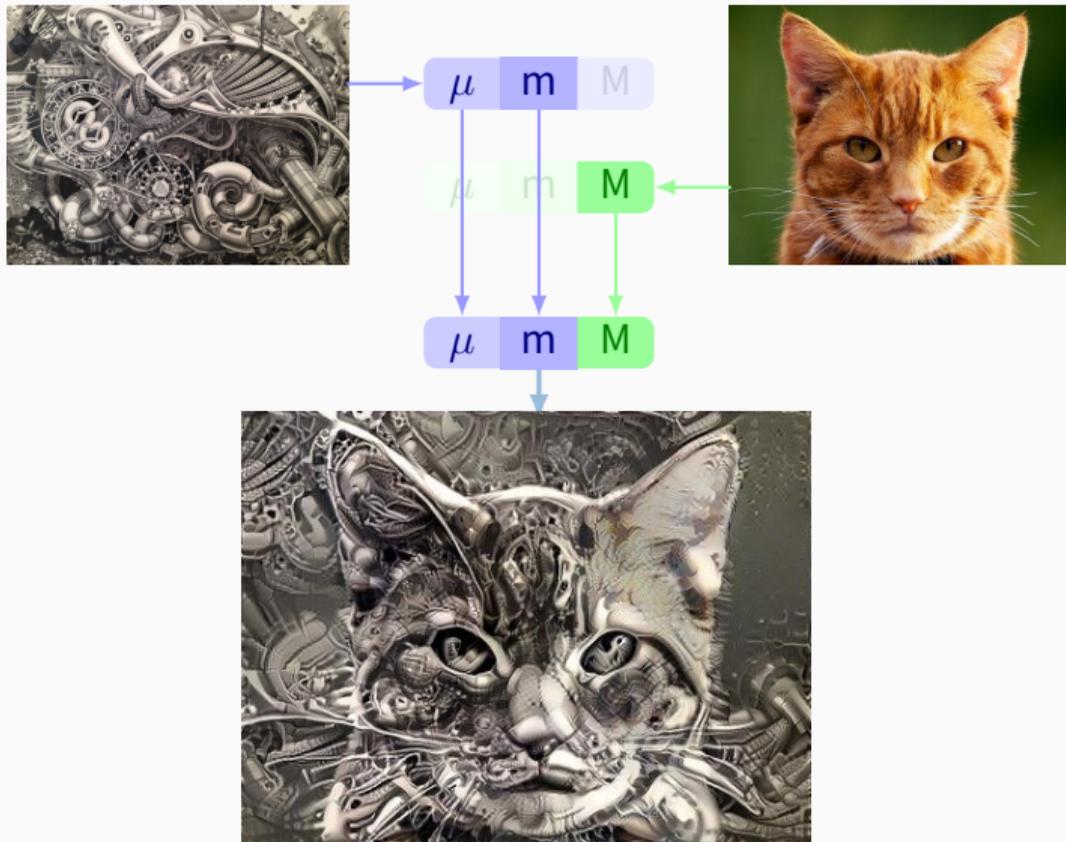
An iconic application: Deep Art [NN16]



An iconic application: Deep Art [NN16]



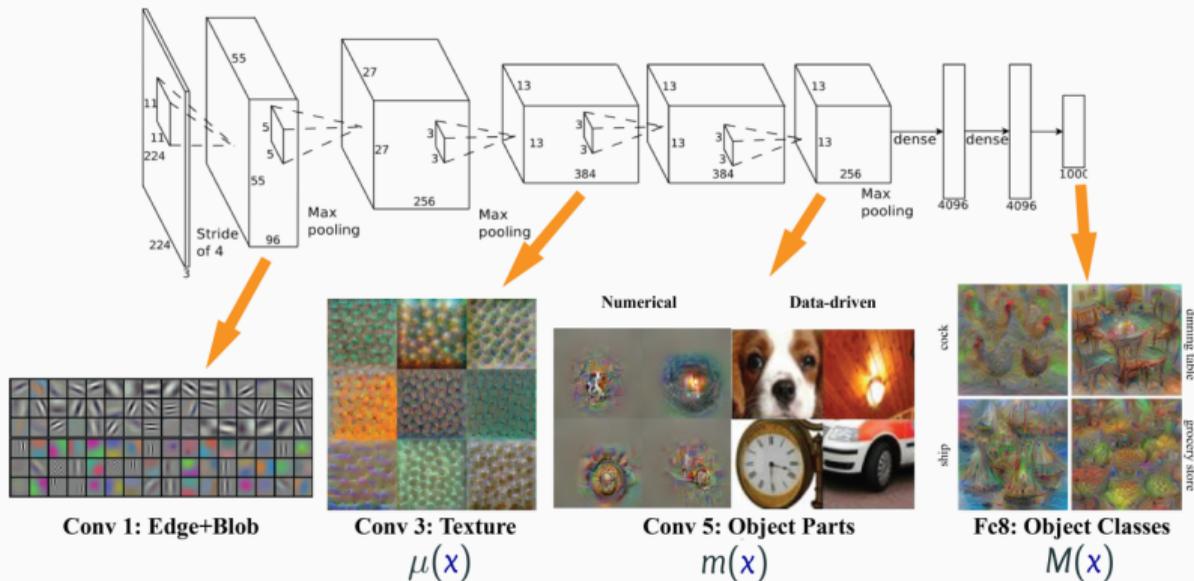
An iconic application: Deep Art [NN16]



The dream application: image classification [WZTF17]

Looking at $\text{CNN}(x) = [\mu(x), m(x), M(x)]$,
can we **distinguish** seagulls from pandas?

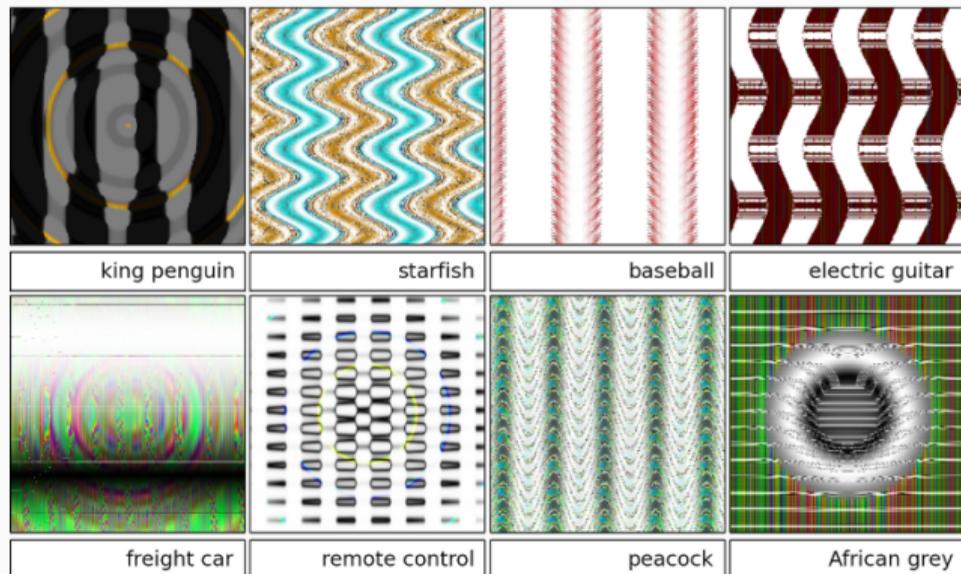
What researchers have in mind:



The limits of multiscale filtering [NYC15]

Standard CNNs perform **pattern detection** – little more, little less:

« $\mu(\mathbf{x})$ is reliable ; $\mathbf{M}(\mathbf{x})$ really isn't. »



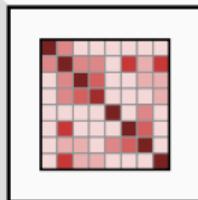
Overview of the class

A geometric perspective on data sciences

Domain-specific observations
on a population of N subjects

MRI/CT images
Cognitive scores
Blood samples
Drug consumption history

N -by- N matrix
of similarities



General machine
learning methods

Clustering (K-Means...)
Classification (hierarchy...)
Regression (kernels...)
Visualization (UMAP...)

This class is about understanding **similarity metrics**.

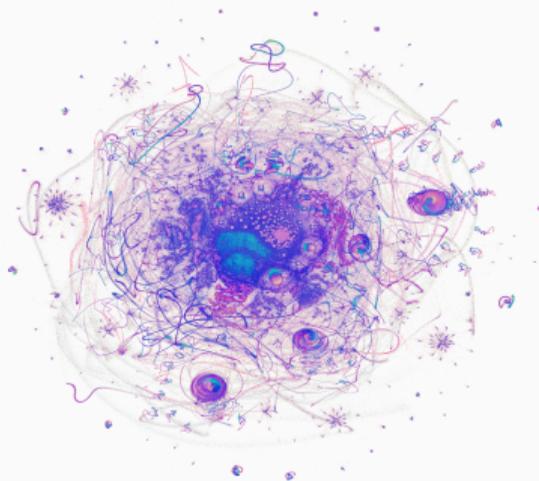
What are the implicit **priors** that they reflect?

How can we manipulate them **efficiently**?

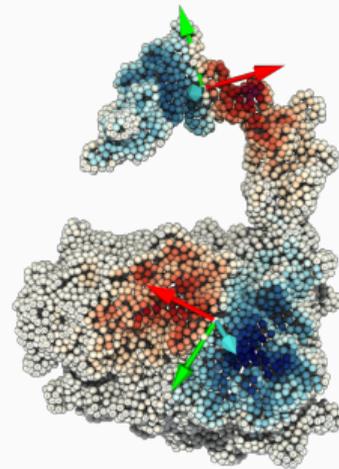
Overview of the class [Wil]



Vectors, linear models
trees and kernels.



Graphs, curvature
and embeddings.



Deep learning: convolutions,
geometry and attention.

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